Java programming for high-performance numerical computing

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First proposed as a mechanism for enhancing Web content, the Java™ language has taken off as a serious general-purpose programming language. Industry and academia alike have expressed great interest in using the Java language as a programming language for scientific and engineering computations. Applications in these domains are characterized by intensive numerical computing and often have very high performance requirements. In this paper we discuss programming techniques that lead to Java numerical codes with performance comparable to FORTRAN or C, the more traditional languages for this field. The techniques are centered around the use of a high-performance numerical library, written entirely in the Java language, and on compiler technology. The numerical library takes the form of the* Array *package for Java. Proper use of this package, and of other appropriate tools for compiling and running a Java application, results in code that is clean, portable, and fast. We illustrate the programming and performance issues through case studies in data mining and electromagnetism.

The Java** language is an attractive general-purpose programming language for many fundamental reasons: clean and simple object semantics, cross-platform portability, security, and an increasingly large pool of adept programmers. In both industry and academia, using the Java language as a programming language for scientific and engineering computations is of great interest. Applications in these domains are characterized by intensive numerical computing. The goal of this paper is to show that the major impediment to the use of Java as a vehicle for numerical computing—performance—is not intrinsic to the language and can be solved using techniques we describe.

It is true that, when commercial Java environments are used, the performance of numerically intensive Java programs falls woefully short of the performance of FORTRAN programs. As shown later in the case study of an electromagnetics application, the performance of numerically intensive Java programs, developed and compiled without the benefit of the techniques described in this paper, can be as low as 1 percent of the performance of equivalent FORTRAN programs. Although anecdotal evidence suggests that performance degradations of up to 50 percent relative to FORTRAN 90 might be tolerated in numerically intensive Java programs in order to gain its other benefits, a 100-fold performance slowdown is unacceptable.

The Java Grande Forum,[1] reflecting in part results from our own research, has identified five critical

Java language and Java virtual machine issues related to the applicability of the Java language to solving large computational problems in science and engineering. Unless these issues are resolved, it is unlikely that the Java language will be successful for numerical computing. The five critical issues are:

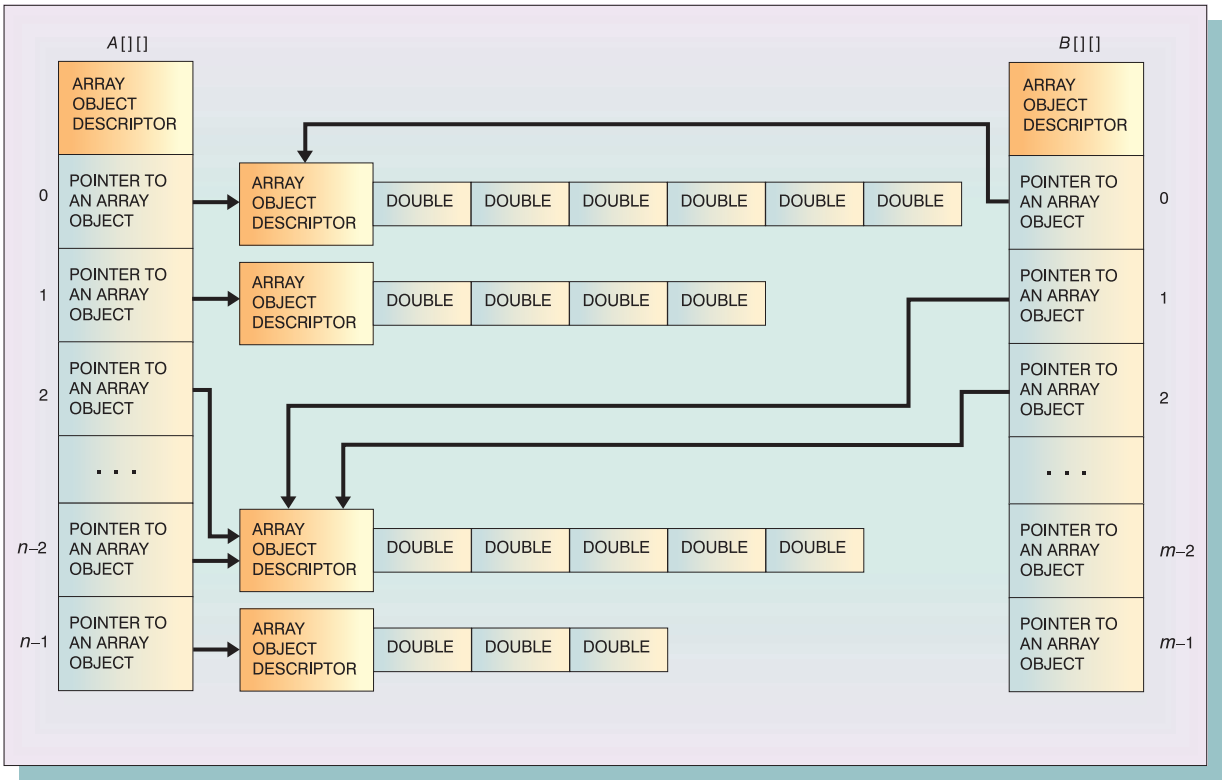
1. Multidimensional arrays—True rectangular multidimensional arrays are the most important data structures for scientific and engineering computing. A large fraction of this paper is dedicated to explaining the problem with the existing Java approach to multidimensional arrays. We also describe our solution to the problem, through the design of a package implemented entirely in the Java language for multidimensional arrays, which we call the *Array package for Java*.
2. Complex arithmetic—Complex numbers are an essential tool in many areas of science and engineering. Computations with complex numbers need to be supported as efficiently as computations with the primitive real number types, float and double. The issue of high-performance computing with complex numbers is directly tied to the next issue.
3. Lightweight classes—The excessive overhead associated with manipulation of objects in the Java language makes it difficult to efficiently support alternative arithmetic systems, such as complex numbers, interval arithmetic, and decimal arithmetic. The ability to manipulate certain objects as having just value semantics is absolutely fundamental to achieve high performance with these alternative arithmetic systems. In this paper, we describe how we were able to treat complex numbers in Java as values, thus achieving FORTRAN-like performance, without making any changes to the language. The same approach can be extended to other numerical types.
4. Use of floating-point hardware—Achieving the highest-possible level of performance on numerical codes typically requires exploiting unique floating-point features in each processor. This exploitation is often at odds with the Java goal of exact reproducibility of results in every platform. In this paper we specifically consider the performance impact of utilizing the POWER and PowerPC* *fused multiply-add* (fma) instruction in Java.
5. Operator overloading—If multidimensional arrays and complex numbers (and other arithmetic systems) are to be implemented in Java as a set of standard packages, then operator overloading is necessary to make the use of these packages more attractive to the application programmer. Although operator overloading is a feature primarily related to code usability and readability, it does have performance implications. We discuss these implications in the context of complex numbers.

This paper discusses our efforts and lists our accomplishments in addressing the performance problems associated with using the Java language for numerical computing. We focus mostly on multidimensional arrays and complex numbers, but our discussion touches all of the previously mentioned five issues. We show that, when our techniques are applied, Java code can achieve between 55 and 90 percent of the performance of highly optimized FORTRAN code in a variety of engineering and scientific benchmarks. We illustrate the details of these performance results through detailed case studies in data mining and electromagnetism. We also provide a summary of results for other benchmarks. The compiler optimizations we discuss have been implemented in our research prototype version of the IBM High-Performance Compiler for Java (HPCJ).[2]

The remainder of this paper is organized as follows. The next section is an overview of the problems associated with the current Java approaches to multidimensional arrays and nonprimitive numerical types. The third section describes the details of the Array package for Java, which supports FORTRAN-like performance for multidimensional array computations in Java code. The subsequent section is a case study of a data mining computation illustrating the performance benefits that result from using the Array package. The fifth section is a case study of an electromagnetics application that makes heavy use of complex numbers. The sixth section summarizes performance results from a larger set of numerically intensive benchmarks, showing that Java implementations can be performance-competitive with the best FORTRAN implementations. The seventh section discusses some related work, and finally, the last section presents our conclusions, discusses the impact of our work, and elaborates on some future research.

The Array package is freely available from alphaWorks*, at http://www.alphaworks.ibm.com/tech/ninja. Our project Web page, with additional information on the Array package and our research in general, is located at http://www.research.ibm.com/ninja.

Figure 1 Example of a two-dimensional Java array



Java approach to multidimensional arrays and complex numbers

In this section, we explain the performance problems associated with the existing Java approaches to implementing multidimensional arrays and alternative arithmetic systems, particularly complex numbers. We also discuss why the corresponding FORTRAN 90 approaches are so much more efficient. We give a taste of our solutions to Java performance problems, which are discussed in more detail in later sections. We show how FORTRAN-like performance can be achieved with 100 percent Java code while remaining within the philosophy and spirit of the language.

Java arrays. Although the specification of Java arrays does not mandate their exact organization, it places sufficient constraints so that all implementations we know of appear as shown in Figure 1. The figure shows how two-dimensional arrays would be laid out, and accessed, in a Java implementation.

The Java language does not directly support arrays of rank greater than one. Thus, a two-dimensional array is represented as an array-of-arrays: an array whose elements are, in turn, references to one-dimensional row arrays. Each array is represented as an *array object descriptor* followed by a chunk of storage that contains the elements of the array. The array object descriptor contains the fields that are present in all objects (lock bits, bits used by the garbage collector, type information, etc.), as well as the upper bound of the array. If a two-dimensional array of type T is being represented, the elements of each row array are either of type T, if T is a Java primitive type, or references to objects of type T. In Figure 1, each element is a Java primitive of type double. Although the layout of the elements of the array are not specified, they are typically contained in a contiguous chunk of storage.

The advantages of this layout for an array are: very general structures can be created, and the necessary

information to perform bounds checking is always available. As seen in Figure 1, it is not required that every row have the same length. Figure 1 is an example of a *ragged* array. It is not even necessary for every row to be unique—rows 2 and $n - 2$ of array A point to the same row array object, and thus $A[2][4]$ and $A[n - 2][4]$ name exactly the same element. Even more generality is possible with arrays of Objects. In that case, each element can be an arbitrary Java object, even another array of any rank and type. All this generality comes with a performance price—a price that is too high for numerical programs that do not need the supplied generality.

First, consider array bounds checking. The Java language specification requires that any access to an array element that is not in bounds must throw an exception. The job of checking for out-of-bounds exceptions exacts a significant toll on Java performance. In Reference 3 it is shown that eliminating array bounds checks alone produced speedups on the IBM POWER and PowerPC processors three to four times over keeping the checks. On some processors, this overhead is less. The real impact on performance, however, comes from having one or more potential exceptions for every data access. Because Java exceptions are precise, operations cannot be moved past a potential exception. This limitation effectively precludes almost all optimizations traditionally applied to numerical programs[4,5]—optimizations that are necessary for good performance.

In Reference 3, techniques for creating program regions free of array bounds exceptions are presented. Even with these techniques, the Java array model interferes with good optimization. Optimizing bounds checks for an array reference $A[i][j]$ inside a loop structure requires: (1) determining the range of values that i and j can take during execution of the loop and (2) being able to test, before starting loop execution, that those ranges will be within the legal bounds of the array. Since a Java two-dimensional array can have rows of different lengths, as shown in Figure 1, the test has to be performed for all rows of the array. A much simpler test could be used if the array were guaranteed to be rectangular (i.e., all rows of the same length).

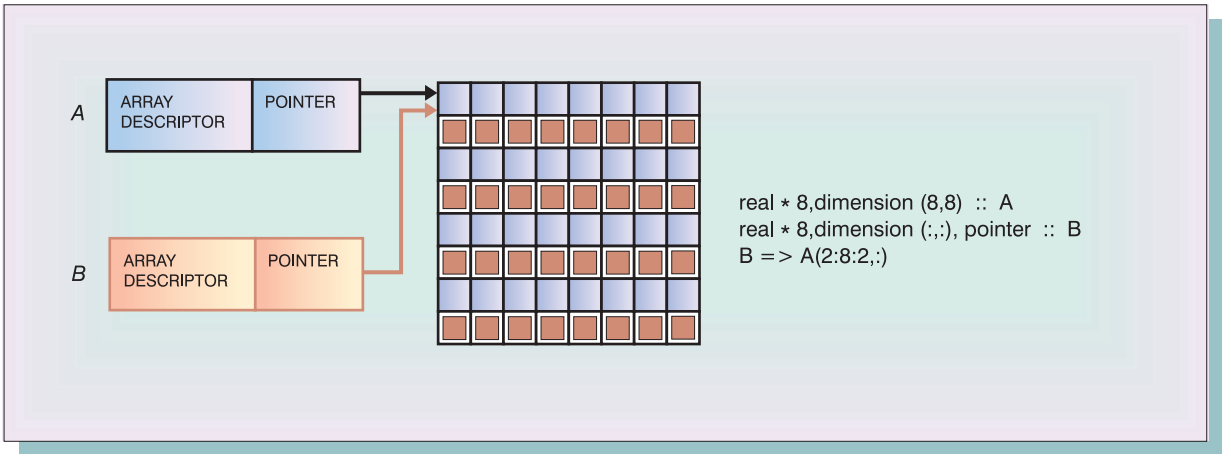
Another major impediment to optimization in Java is the ability to alias rows of an array. Aliasing occurs when two or more apparently different variables or references actually refer to the same datum. An example of aliasing is shown in Figure 1, where $A[2]$ and $A[n - 2]$ refer to the same row. Moreover, $B[1]$, $B[2]$, $A[2]$ and $A[n - 2]$ all refer to the same row. The problem with aliasing is that many optimizations rely on moving data reads and writes relative to one another. For this rearrangement to be legal, it is necessary that (1) all writes to a datum be kept in order; (2) that no write to a datum be moved prior to a read of the same datum; and (3) that no read from a datum be moved after a write to the same datum. Essential to determining the legality of a transformation is the ability to determine when two operations are to different data and, therefore, independent. Aliasing makes this more difficult because it is no longer possible to say that just because two variables have different names, or because different array elements have different coordinates, they must refer to different memory locations.

The final problem with Java arrays that we discuss is the cost of accessing an element. Accessing element $A[2][4]$ requires the following steps: (1) get the reference to the array object A; (2) determine that A is not a **null** pointer; (3) determine that "2" is an in-bounds index for A; (4) get the reference to the array object that is row 2; (5) determine that this object reference is not a **null** pointer; (6) determine that "4" is an in-bounds index for $A[2]$; and (7) get the data element $A[2][4]$. In contrast, as we will see, FORTRAN 90 requires only two steps.

FORTRAN 90 arrays. The structure of a FORTRAN 90 two-dimensional array is shown in Figure 2. It has two major components: a block of dense, contiguous storage that holds the data elements of the array, and a *descriptor* that contains the address of the block of dense storage, bounds information for each dimension, the size of individual data elements, and other information used to index the array. This indexing information is used to access array elements and implement array sections. Accessing an element of the array is straightforward: the base address of the storage is extracted from the descriptor, and the subscript, along with the indexing information contained in the descriptor, is used to compute an offset into the data storage.

Because of the information contained in the descriptor, array sections (see array B in Figure 2, which corresponds to the shaded elements of A) can be implemented efficiently. A *section* of a FORTRAN 90 array A is a view of A that accesses some subset of the elements of A. The section has the following properties: (1) it (logically) utilizes the same storage as the original array, thus a change of an ele-

Figure 2 The layout of a FORTRAN 90 array



ment value contained in A and the section is reflected in both; (2) the section has rank less than or equal to the rank of A; (3) the elements in the section are defined by enumerating element indices along each axis; and (4) each element enumerated must be a valid, in-bounds element of the original array axis. Let A be an array of shape 8×8. Then $B \Rightarrow A(2:8:2,:)$ associates B with rows 2, 4, 6, 8, and all columns of the original array A. The reference $B(3,4)$ accesses row 6 and column 4 of the original array A. This example is illustrated in Figure 2.

The design of FORTRAN 90 arrays has several advantages. First, because the storage is dense and contiguous, access requires a single pointer dereference and offset computation, regardless of the rank or dimensionality of the array being accessed. Second, the ability to take sections allows great flexibility in passing portions of arrays to library functions. Third, a rich set of *intrinsic functions* (i.e., built-in operators expressed syntactically as functions) that operate on arrays can be supported. Fourth, most primitive operations in the language (e.g., $+$, $-$, $*$, and $/$) are overloaded and specify the operation applied elementwise over the entire array. Finally, despite its support of array sections, aliasing disambiguation with FORTRAN 90 arrays is much simpler than with Java arrays. Given two two-dimensional FORTRAN 90 array sections $A(l_A^1 : u_A^1 : s_A^1, l_A^2 : u_A^2 : s_A^2)$ and $B(l_B^1 : u_B^1 : s_B^1, l_B^2 : u_B^2 : s_B^2)$, alias disambiguation is a matter of showing that $A \neq B$ or that the intersection of the ranges is empty: $(l_A^1 : u_A^1 : s_A^1) \cap (l_B^1 : u_B^1 : s_B^1) = \emptyset$ or $(l_A^2 : u_A^2 : s_A^2) \cap (l_B^2 : u_B^2 : s_B^2) = \emptyset$. Even if disambiguation cannot be done at compile time, the run-time test is trivial. In comparison, the disambiguation of two two-dimensional Java arrays, with their unrestricted pointers as shown in Figure 1, is almost always impossible at compile time (without extensive interprocedural analysis) and very expensive at run time.

FORTRAN 90 arrays are not, however, without their faults. *Storage association* exposes the programmer to the fact that data elements are contiguous in memory, and that the next logical element of the array is also adjacent in storage to the previous element. Quite frequently, FORTRAN programs rely on storage association to execute correctly. In addition, optimizations that alter the layout of an array[6–9] are globally visible. As a consequence, data typically have to be copied to and from the original layout. Copying makes these optimizations more fragile and less useful, since the overhead of copying the arrays twice must be factored into the cost model for determining whether the optimization should be performed.

A solution for true multidimensional arrays in Java. To overcome the performance deficiencies inherent to Java arrays, we developed the Array package for Java. The Array package is a class library that implements true rectangular multidimensional arrays that combine (1) the efficiency of FORTRAN 90 arrays, (2) the flexibility of data layout of Java arrays, and (3) the safety and security features provided by the Java requirement for bounds checking. With the Array package, multidimensional arrays are created

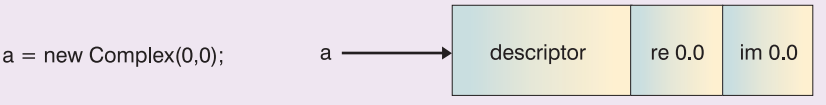
Figure 3 A standard Java class for complex numbers

```
public final class Complex  {

     public double re,  im;

     public Complex(double r, double i)  { re = r; im = i;  }
     public Complex assign(Complex z)  { re = z.re; im = z.im; return this;  }
     public Complex plus(Complex z)  { return new Complex(re+z.re,im+z.im);  }
     public Complex minus(Complex z)  { return new Complex(re–z.re,im–z.im);  }
     public Complex times(Complex z)  {
          return new Complex(re*z.re–im*z.im,im*z.re+re*z.im);
     }
     public Complex times(double x)  { return new Complex(re*x,im*x);  }
     public Complex plusAssign(Complex z)  { re += z.re; im += z.im; return this;  }
}
```

(A) Code for Complex class



(B) Complex object creation and representation

using standard Java constructs. For example, the code

```
doubleArray2D A = new doubleArray2D(m,n);
doubleArray2D B = new doubleArray2D(m,n);
```

declares two two-dimensional arrays A and B of (rectangular) shape $m \times n$. Elements of these arrays can be accessed using set and get methods from the class doubleArray2D. For example,

```
A.set(j,i,B.get(i,j));
```

copies element (i, j) of array B into element (j, i) of array A. A more detailed description of the Array package appears in the next section. For now, suffice it to say that the Array package has FORTRAN-like semantics to facilitate compiler optimizations.

Complex numbers in the Java and FORTRAN 90 languages. In the FORTRAN programming language, complex numbers are supported as primitive types. Arithmetic operations with complex numbers can be coded as easily as with real numbers. Multidimensional arrays of complex numbers are directly supported in FORTRAN. Java, in contrast, does not support primitive complex types. The typical approach for implementing complex numbers and complex arithmetic in Java is through the definition of a Complex class. Some components of such a class, which is being proposed for standardization by the Java Grande Forum,[1] are shown in Figure 3. Objects of this class are used to represent complex numbers. We note that a Complex object typically requires 32

bytes for representation: a 16-byte object descriptor (present in all Java objects) and two 8-byte fields for the real and imaginary parts.

The operation $a \times b + c$, where a, b, and c are complex numbers, can be coded in Java as

```
a.times(b).plus(c)
```

where a, b, and c are references to objects of class Complex. Note that the evaluation of a.times(b) creates a new Complex object to hold this intermediate result. Method plus is then invoked on this intermediate result, creating yet another object with the result of $a \times b + c$.

The approach of representing complex numbers as objects of class Complex, and the associated creation of objects to represent the output of computations, results in a very high cost for using complex numbers in Java. As seen in the MICROSTRIP benchmark results (in the case study on electromagnetics, where a detailed analysis of this benchmark is given), applications using a Java Complex class (to represent complex numbers) can be 100 times slower than the equivalent applications in FORTRAN 90. These performance problems can be addressed by using the technique of *semantic expansion*,[10] as implemented in our research prototype HPCJ.

Semantic expansion treats standard classes as language primitives. Unlike traditional procedure or method "inlining," which (intuitively) treats the inlined method as a macro, semantic expansion uses the compiler's built-in knowledge of the class semantics to directly generate efficient, legal code. With semantic expansion, Complex objects and operations on those objects are recognized by the compiler and treated essentially as language primitives (largely as FORTRAN 90 would treat them). The arithmetic methods of class Complex are treated by semantic expansion as operating and returning *complex values* (pairs of [*real*, *imaginary*] doubles). If the consumers of theses values are other arithmetic methods of Complex, they are semantically expanded to directly use the complex values. That is, only the resulting value of an operation is propagated from one step to the next. Otherwise, the value is converted to a Complex object, with all the properties of a regular Java object. By treating complex numbers as values whenever possible, temporary Complex objects do not have to be created for arithmetic operations, thus reducing the allocation and garbage collection overhead. This approach delivers the same performance benefit for complex numbers as the proposed *value object* extension for Java,[1] without requiring language changes. We show in the section on the electromagnetics case study and in the subsequent section that semantic expansion can sometimes improve the performance of Java applications using complex arithmetic to approximately 80 percent of the performance of corresponding FORTRAN 90 programs.

The problems we described earlier associated with Java multidimensional arrays are exacerbated with arrays of complex numbers. A Java two-dimensional array of Complex, declared as Complex[ ][ ] C, is just a collection of pointers to Complex objects. Optimizing **null**-pointer checks requires, in general, an inspection of the entire array. In addition to the indiscriminate row-level aliasing shown in Figure 1, Java arrays of Complex objects are subject to indiscriminate *element-level aliasing*, making the issue of alias disambiguation even harder.

We address the problems related to Java arrays of complex numbers by including in the Array package classes that represent true rectangular arrays of complex numbers (e.g., ComplexArray2D). These arrays always have a complex number associated with each element, and there is no aliasing between two different elements.

The role of operator overloading. The Array package, the Complex class, semantic expansion, and other compiler techniques we developed can successfully achieve high levels of performance with numerical computing in Java. However, we are still left with the difficulty of writing, maintaining, and reading programs that make extensive use of classes to represent numerical and array types. Some form (maybe limited) of operator overloading is necessary to allow application programmers to write their codes in a clear and intuitive notation. At a minimum, it is necessary to support operator overloading of the basic arithmetic ($+$, $-$, $*$, $/$, $\%$) and relational ($==$, $!=$, $<=$, $<$, $>$, $>=$) operators, as well as of the array indexing operator ([ ]).

As an example, consider the evaluation of $b[i, j] = a[i + 1, j] + a[i - 1, j]$, where b and a are two-dimensional arrays of complex numbers (implemented as ComplexArray2D). Ideally, we would like to code this operation as

```
b[i,j] = a[i+1,j] + a[i-1,j]                    (1)
```

which is an operator-overloaded representation for

```
b.set(i,j,a.get(i+1,j).plus(a.get(i-1,j)))        (2)
```

The set and get methods correspond to the overloaded array indexing operator ([ ]) and the plus method corresponds to the overloaded addition operator (+). Operator overloading is fundamental for productivity and clarity of numerical codes using nonprimitive arithmetic systems and array classes. (An alternative to defining operator overloading in the language is to make use of visual editors that present a more convenient interface to numerical programmers. Unfortunately, it binds the programmer to a particular development environment.)

Operator overloading also has an impact on performance. Rules for the semantics of operator overloading must be simple, and code written with overloaded operators (e.g., code fragment 1) is typically equivalent to code that creates temporary objects (e.g., code fragment 2). In other words, object reuse in code with overloaded operators is difficult. Thus, the kind of optimizations through semantic expansion that we describe for complex numbers is even more important.

The Array package for Java

The goal of the Array package for Java is to overcome the limitations inherent in Java arrays in terms of performance and ease of use, as compared to array implementations in other languages. A major design principle of the Array package is to define a set of classes implementing FORTRAN 90-like multidimensional arrays that are highly optimizable, amenable to compiler analysis techniques, and that contain the functionality necessary for numerically intensive computing. We have modeled the Java Array package along features of the FORTRAN 90 language[11] and the A++/P++ libraries.[12,13] Not surprisingly, the reader will also find similarities with APL, since that programming language undoubtedly influenced the design of FORTRAN 90. However, APL is a much more dynamic language, with strong support for polymorphism of data and functions. The design of the Java Array package, particularly as described in this paper, follows the more static nature of FORTRAN 90. This design allows us to leverage mature compiler technologies that have been developed for FORTRAN over the course of many years. It is important to emphasize that the Array package is written entirely in the Java language. Its use does not require any code preprocessing steps, just the appropriate import statements.

A word about notation: From now on, when we use the term *Array* (with an uppercase *A*) we refer to the constructs provided by the Array package. The standard arrays in the Java language will be referred to as *Java arrays* (with a lowercase *a*).

The functionality provided by the Array package is implemented by a set of basic methods and operations that are highly optimizable. The class hierarchy inside the Array package has been defined to enable aggressive compiler optimization. As an example, we make extensive use of *final* classes, since most Java compilers (and, in particular, *javac*) are more easily able to apply method inlining to methods of final classes. This approach also statically binds the semantics of methods, thus facilitating semantic expansion. In the most commonly used methods of the Array package (i.e., simple element-wise operations) the cost of a method call dominates the cost of the computation done by the method. Therefore, inlining those methods is essential for good performance.

In contrast to Java arrays discussed in the previous section, Arrays defined by the Array package have properties (e.g., a nonragged rectangular shape and constant bounds over their lifetime) that are easy to detect and use by an optimizing compiler. Thus, for problems that map well to rectangular multidimensional structures, the Array package provides both functionality and performance and is the obvious choice over Java arrays.

Arrays are *n*-dimensional rectangular collections of elements. An Array is characterized by its *rank* (number of dimensions or axes), its elemental data *type* (all elements of an array are of the same type), and its *shape* (the extents along its axes). Rank, type, and shape are immutable properties of an Array. All Array classes are named using the following scheme: ⟨*type*⟩Array⟨*rank*⟩D. As an example, floatArray3D is a three-dimensional Array of single precision floating-point numbers. In the current version of the Array package, *type* can be any of the Java primitive types (boolean,byte,char,short,int,long,float,double), Complex (for complex numbers), or Object for general objects. The currently supported values for *rank* are 0, 1, 2, and 3.

Class hierarchy. All Array classes are derived from a base abstract class Array, which defines the common methods for all types of Arrays. Arrays are further subdivided according to their (elemental) type and rank. We also define the Index and Range helper

classes for indexing and sectioning an Array (see the later subsection on indexing for more details). Various exception classes are also provided by the Array package for reporting errors that occur during array operations. Figure 4 shows the class hierarchy of the Array package.

We note that the fully qualified name of the Array package for Java, in accordance with Java standards, is com.ibm.math.array. Use of this fully qualified name allows us to build knowledge about the Array package into our compiler.

Transactional behavior, array semantics, and exceptions. All operations (methods and constructors) of the Array package have, in the absence of Java virtual machine (Jvm) failure, transactional behavior. That is, only two outcomes of an array operation are possible: (1) the operation completes without any error, or (2) the operation is aborted, in which case an exception is thrown before any user-visible data are changed.

If a Jvm failure occurs (e.g., it runs out of stack space) during the execution of an Array package operation, the program enters an unrecoverable error state, and the results of the partial operation are observable only by postmortem tools. Therefore, the fact that the transactional behavior is violated in this particular case is irrelevant.

In order to clearly identify what was the cause for aborting an Array package operation, exceptions are thrown. These exceptions have descriptive names that make the cause of the exception clear to the user. For example, a NonconformingArrayException is thrown if the user attempts to add two Arrays of different shapes, indicating that the add operation cannot be performed because the Arrays do not match. Other exceptions are thrown in other scenarios. The number of methods that might throw a particular exception is very large, so we do not cover all cases extensively in this paper.

All exception classes are derived from the RuntimeException class. In Java, exceptions derived from the RuntimeException class are not required to be caught by user code. Hence, it is not an error for a piece of code to invoke an Array package method but not declare (using a throws clause) or catch an exception that may be thrown by that method. In current numerical algorithms, conditions that would raise an exception typically result from programming bugs. The expectation is that the programmer will fix the bug rather than add exception-handling code to handle it at run time. Nevertheless, if the programmer would like to catch the exception, it can still be done, and so no limitations have been placed on exception handling.

Array operations also implement *array semantics*: In evaluating an expression (e.g., $A = A * B + C$), all data are first fetched (i.e., A, B, and C are read from memory), the computation is performed (i.e., $A * B + C$ is evaluated), and only then are the results stored (i.e., A is modified). Of course, a high-performance system should implement array semantics while optimizing to avoid unnecessary copying. (See the subsection on internal optimizations for more details.)

Array constructors. The shape of an array is specified at its creation through a constructor, and it is immutable. The Array package defines three constructors for each Array class, illustrated in Figure 5. The first constructor shown builds a new Array whose shape is specified by the parameters. The second constructor shown builds a new Array that is a copy of the Array input parameter. The new Array has its own storage and shares no data with the input Array. Finally, the third constructor shown builds a new Array with elements copied from a conventional Java array. If the Java array is multidimensional, it must be rectangular. Again, the new Array has its own storage area.

Indexing elements of an array. Elements of an array are identified by their indices (coordinates) along each axis. Let a k-dimensional array A of elemental type T have extent n_j along its jth axis, $j = 0, \ldots, k - 1$. Then, a valid index i_j along the jth axis must be greater than or equal to zero and less than n_j. An attempt to reference an element $A[i_0, i_1, \ldots, i_{k-1}]$ with any invalid index i_j causes an ArrayIndexOutOfBoundsException to be thrown.

The Array package allows an axis of an Array to be indexed by either an integer, a Range object or an Index object. Indexing with an integer specifies a single element along an axis. Indexing with a Range object is like addressing using triplets in FORTRAN: a first element, a last element, and an optional stride (which defaults to one) specify a regular pattern of elements. An Index object is a list of numbers that is used by the Array package method to select the enumerated elements along the given axis. Index objects are convenient for scatter-gather operations and for operations on sparse data in general. When in-

Figure 4 Simplified class hierarchy chart

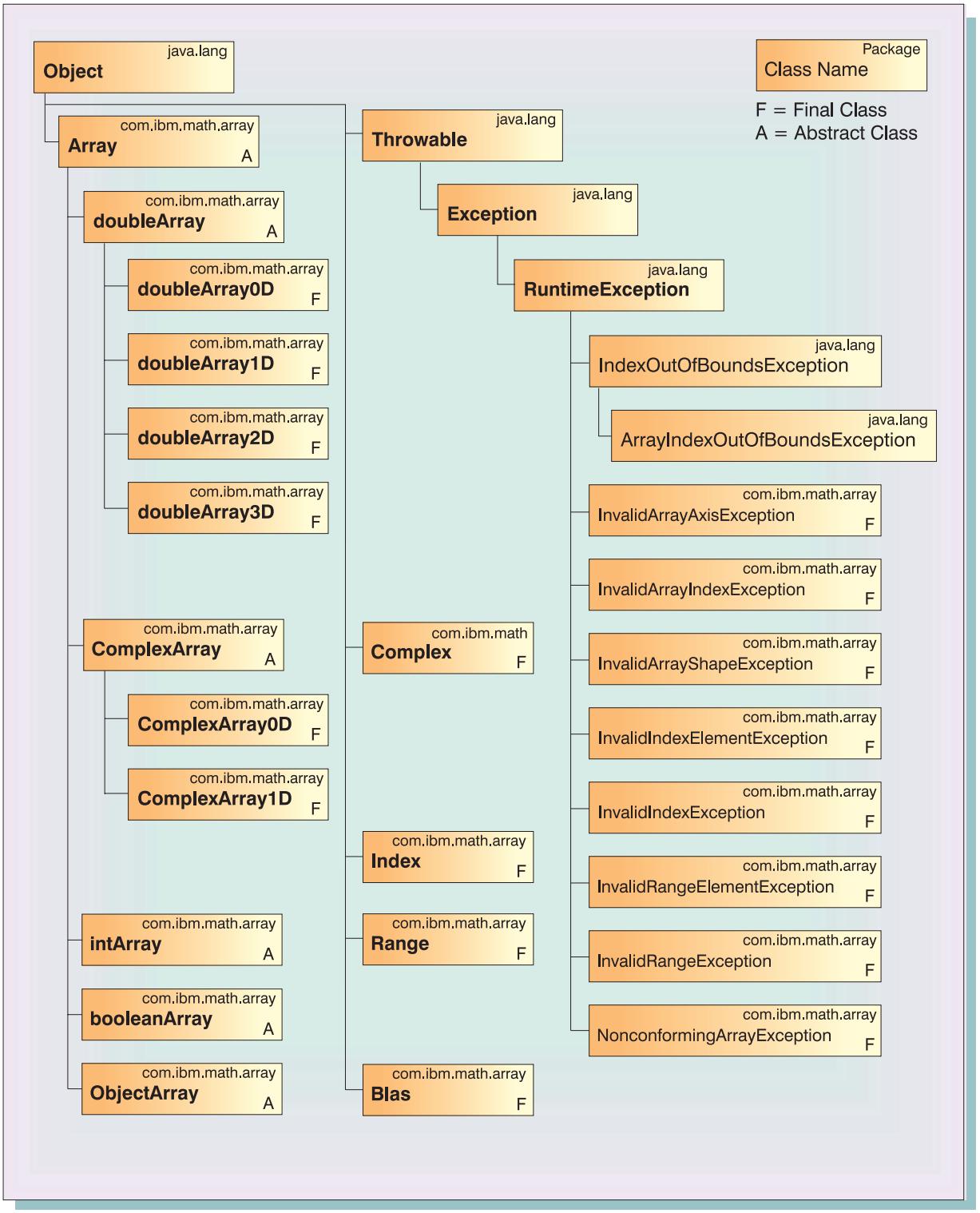


Figure 5 Simple Array construction operations

```
// Simple 3 x 3 array of integers
intArray2D A = new intArray2D(3,3);

// This new array has a copy of the data in A,
// and the same rank and shape.
intArray2D A2 = new intArray2D(A);

// Java array of bytes
byte[] buffer = { 0x1A, 0x20, 0xCA, 0xFE, 0x01 };

// New byte array with the same data
byteArray1D B = new byteArray1D(buffer);
```

dexing with an Index or Range object, all the indices must be valid (i.e., within bounds), or an ArrayIndexOutOfBoundsException is thrown.

Indexing operations are used in *accessor methods* that read or write data from or to an array, and in *sectioning methods* that create views of an array. Accessor methods support all possible combinations of integer, Range, and Index indices. That is, the subscript along any given dimension can be either an integer, a Range object, or an Index object. Sectioning methods only support combinations of integer and Range indices. Supporting sections defined with Index objects would require a complicated and slow descriptor for the Array and impair efficient access to Array elements in the common cases. Array accessors can be implemented efficiently even with Index objects.

Defined methods. The Array package defines four groups of methods that are always present in any Array package class: Array operation, Array manipulation, Array accessor, and Array inquiry. A group of methods is just a collection of methods with similar functionality. The complexity of operations is, in most cases, similar for methods of a group.

Array operations. Array operations are scalar operations applied element-wise to a whole Array. The methods in this category include assignment, arithmetic and arithmetic-assign operations (analogous, for example, to += and *= operators in Java), relational operations, and logic operations (where appropriate for the elemental data type). These operations are further subdivided as *Scalar-Array* and *Array-Array* operations. Scalar-Array operations apply the operation to a scalar and each element of the Array. Array-Array operations apply the operation to all equivalent elements of two Arrays. If both Arrays in an Array-Array operation do not have the same shape, a NonconformingArrayException is thrown. These operations are highly optimizable and parallel in nature.

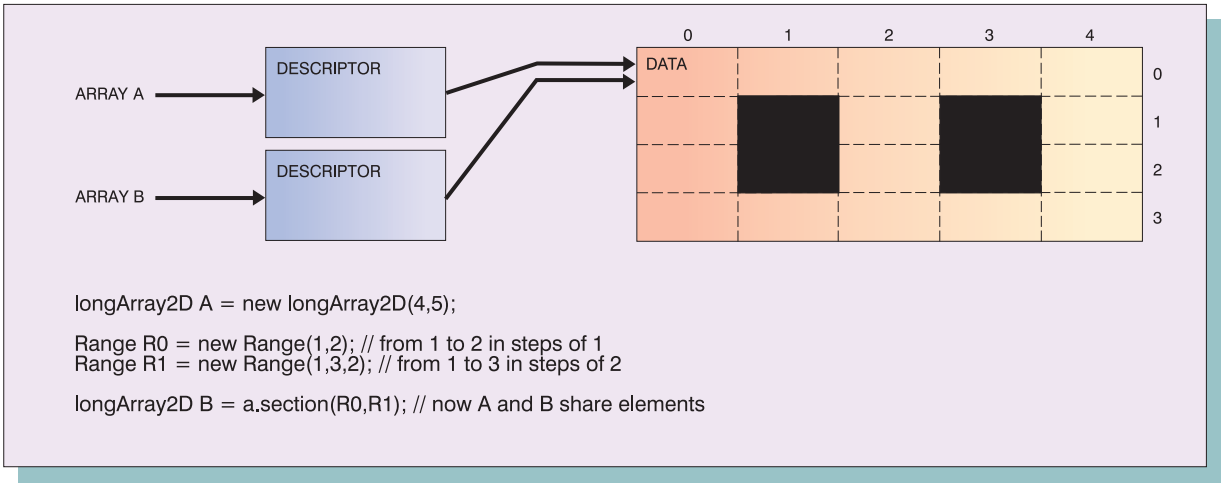
In Figure 6 we compare some elementary Array operations described using a math notation and the notation defined by the Array package. When there is more than one Array package version for the expression, the first expression is the most straightforward and intuitive form. The alternative forms for an operation lead to better performance, as they avoid creating (at least some) intermediate objects. (The forms are semantically equivalent, if the whole operation is legal.) It is unrealistic to expect users of the Array package to write all Array expressions in the less intuitive but more efficient form. An intelligent compiler should be able to automatically translate the Array expressions to the best-performing version.

Array manipulation. Methods in this group include section, permuteAxes, and reshape. These methods operate on the array as a whole, creating a new view of the data and returning a new Array object express-

Figure 6 Array operations in Array package and math notations

Math Notation	Java Array Package Notation
$A \leftarrow B$	A.assign(B);
$A \leftarrow A + B$	A.assign(A.plus(B)); A.plusAssign(B);
$A \leftarrow B + C \times D$	A.assign(B.plus(C.times(D))); A.assign(C).timesAssign(D).plusAssign(B); C.times(D,A).plusAssign(B);
$A \leftarrow 0.25\ (B + C + D + E)$	A.assign(B.plus(C).plus(D).plus(E).times(0.25)); A.assign(B).plusAssign(C).plusAssign(D).plusAssign(E).timesAssign(0.25); B.plus(C,A).plusAssign(D).plusAssign(E).timesAssign(0.25);

Figure 7 Example of an array section—a 2 x 2 Array B associated with rows 1 and 2 and columns 1 and 3 of Array A



ing this view. A new Array object is needed because an Array object always has constant properties, and the new Array view may have different basic properties than the original array (e.g., a different rank or shape). This new Array object shares its data with the old object when possible to avoid the overhead of data copying.

Sectioning an Array means obtaining a new view to some elements of a given Array. A section is a new Array object that shares its data with the original Array, as a FORTRAN 90 section shares its data with the base array. Since data are shared, only a descriptor needs to be created, resulting in a fast sectioning operation. Figure 7 illustrates how a sectioning operation works. For two-dimensional Arrays, the first index applies to rows, and the second index applies to columns. This example creates a section B corresponding to rows 1 and 2 and columns 1 and 3 of A. Because sections are first-class Array objects, operating on an Array section is indistinguishable from operating on any other Array object.

Figure 8 Permuting axes, with and without data copy

```
// Create a 5x4 Array A of longs
longArray2D A = new longArray2D(5,4);

// Create an Array B that is a transpose of A. This is just a
// descriptor operation. The internal data layout of
// A is not changed. The data in A is shared with B.
longArray2D B = A.permuteAxes(1,0);

// Use the copy constructor to guarantee that the data are copied.
// C has a copy of the data in A, but with a different organization.
longArray2D C = new longArray2D(A.permuteAxes(1,0));
```

The permuteAxes method implements generic axis interchange. Although permuteAxes(1,0) returns a transposed two-dimensional array, permuteAxes is more general than a simple transpose because any axis can be replaced by any other axis, as long as all axes that exist in the original Array also exist in the permuted Array. If this condition is not met, the method call is illegal and an exception is thrown. For example, B = A.permuteAxes(2,1,0) exchanges axes 0 and 2 of a three-dimensional Array A. That is, B(i,j,k) = A(k,j,i). The expression B = A.permuteAxes(1,1,0) is illegal, and throws a run-time InvalidArrayAxisException, since axis 1 appears twice and axis 2 is missing. Permuting the axis of a given array is a fast operation that only creates a new descriptor. No data copy is needed as the data are shared with the original array. If the user wants data copy to take place, the copy constructor always guarantees that the data are actually copied, as in the example in Figure 8.

The reshape method returns a new Array with the same data as the old Array but with a different shape. Every element in the old Array is mapped to an element of the new Array. Therefore, the new Array has the same number of elements as the old Array. The algorithm used to map Array elements is the following. The data are first (logically) linearized by visiting all axes in order and all elements within an axis in index order. The logically linearized elements are then copied into a new Array with the shape specified in the reshape call, again by visiting all axes and all elements within an axis in order. Figure 9 gives examples of reshape method calls. The reshape method throws an InvalidArrayShapeException if the specified shape does not have the right number of elements.

Because Array objects have immutable shape, reshaping an Array implies creating a new Array object. A copy of data is needed because our descriptor, which is designed to be fast for common operations, is not rich enough to express the effect of a reshape. We choose not to have a complex descriptor that supports fast reshaping for two reasons: First, the complex descriptor would slow down most other methods. Second, a common purpose of an Array reshape operation is to reorganize the data in order to obtain faster access, and so data copying is a desirable consequence of the reshape operation.

Array accessor methods. The methods of this group are get, set, and toJava. These are methods that allow the user to extract and change the array data. Figure 10 contains examples of uses of the methods in this group. The get and set methods are straightforward. The programmer is provided indexing methods (described earlier) to select one or more elements. A get returns the specified elements, and a set updates the specified elements. The method toJava allows a user to extract a Java array from an Array package Array. This feature, together with constructors that convert Java arrays into Array package Arrays, allows pieces of

Figure 9 Reshaping an array

```
short [] [] JavaArray = {  {1,2}, {3,4}, {5,6}  };

shortArray2D A = new shortArray2D(JavaArray);

shortArray2D B = A.reshape (2,3);
// B is now  {  {1,2,3},{4,5,6}  }

shortArray1D C = B.reshape(6);
// C is now  { 1,2,3,4,5,6 }

shortArray2D D = C.reshape(3,2);
// D is equal, in value, to A. The reshape never
// changes the defined total order among elements
```

Figure 10 Simple Array accessor operations

```
doubleArray2D A = new doubleArray2D(5,5);

// Simple element wise operations
double firstElement = A.get(0,0);
A.set(4,4,firstElement);

// The row1 Object has a copy of the data in the first row of
// array A. it is not a section of Array A because it does
// not share data with A.
doubleArray1D row1 = A.get(0,new Range(0,A.last(1)));

// The second row of array A now equals the first (values, not aliased)
A.set(1,new Range(0,A.last(1)),row1);

// Extract elements of A into a double [] [] structure
double [] [] AJava = A.toJava( );
```

code that work with Java arrays to coexist with (i.e., exchange data with) pieces of code that use the Array package.

Because the basic purpose of this group of methods is to move data in and out of Arrays, data copy is always performed. The common operations are fast—for example, extracting a single element from an array. Extracting an entire subarray (e.g., a row of a two-dimensional array) using a single Array class operation is typically faster than extracting one element at a time.

Figure 11 Side-by-side comparison of FORTRAN 90 and Array package for Java constructs

FORTRAN 90	Java Array Package

INTEGER : : m,n,p
ALLOCATABLE, REAL*8 : : a(:,:), b(:,:), c(:,:)
ALLOCATE (a(0:m–1,0:p–1))
ALLOCATE (b(0:p–1,0:n–1))
ALLOCATE (c(0:m–1,0:n–1))
 	
c(i,j) = c(i,j)+a(i,k)*b(k,j)
 	
c(0:10,0:p–1) = b(10:20,0:p–1)
 	
INTEGER, DIMENSION(10) :: I, j
REAL*8, DIMENSION(0:9,0:19) :: x, y
i = (/ 2, 3, 5, 7 /)
j = (/ 1, 2, 4, 8 /)
x(i,0:19) = y(j,0:19)
	int m, n, p;
	doubleArray2D a, b, c;
	a = new doubleArray2D(m,p);
	b = new doubleArray2D(p,n);
	c = new double Array2D(m,n);
	
	c.set(i,j,c.get(i,j)+a.get(i,k)*b.get(k,j));
	
	Range pm1 = new Range(0,p–1);
	Range R010 = new Range(0,10);
	Range R1020 = new Range(10,20);
	c.section(R010,pm1).assign(b.section(R1020,pm1));
	
	Index I, j;
	doubleArray2D x, y;
	i = new Index (...);
	j = new Index (...);
	x = new doubleArray2D(10,20);
	y = new doubleArray2D(10,10);
	x.set(i,new Range(0,19), y.get(j,new Range(0,19));

Array inquiry methods. This group contains methods last, size, rank, and shape. They are fast, descriptor-only operations that return information about the constant properties of the Array.

The method last (used as an example in Figure 10) returns the last valid index along a given axis. The method size, when invoked without arguments, returns the number of elements in the Array; if invoked with an int argument, it returns the number of elements along this given axis. The method rank returns the rank of the Array (i.e., the number of axes or dimensionality of the Array). Finally, the shape method returns a Java array of integers whose elements are the sizes of the Array along each individual axis.

Comparing array operations in FORTRAN 90 and with the Array package for Java. As previously mentioned, we have patterned our design of the Array package along the lines of the FORTRAN 90 language. Figure 11 provides a side-by-side comparison of equivalent FORTRAN 90 and Java Array package constructs. Readers familiar with FORTRAN 90 will notice an almost one-to-one correspondence between the two approaches. This correspondence has both performance as well as usability implications. From a performance perspective, optimization techniques developed for FORTRAN 90 can be applied to the Array package. From a usability perspective, programmers used to FORTRAN 90 features will find corresponding functionality in the Array package.

Internal optimizations. The semantics of Array operations imply that they are performed on Arrays as they would be performed on scalars. That is, the result is computed before assignment into the target array. Therefore, execution of an Array operation logically follows the sequence: (1) all operands are fetched from memory, (2) all computation is performed, and (3) the result is stored to memory. The ordering between steps (2) and (3) implies that, in general, the result of the operation must be first stored in a temporary Array and then copied to the final target.

Figure 12 Example of array operation internally optimized through dynamic data dependence analysis

```
floatArray2D x;
floatArray1D row1 = x.section(1,new Range(0,x.last(1)));
floatArray1D row2 = x.section(2,new Range(0,x.last(1)));

row1.plusAssign(row2);
```

To provide good performance, the supplied Array operations avoid data copying—a costly operation—as much as possible. For example, consider the code in Figure 12. A naive implementation would perform the plusAssign method in two steps: First, a new Array object is created to store the sum of the two Arrays. Then, the contents of the new object are copied back to the first Array. The unnecessary copying degrades performance. The result of an Array operation can be written directly to the target Array (thus eliminating the need for the temporary Array and the copy operation) if doing so does not overwrite any memory location before its use as an operand. The Array package uses a form of dynamic *dependence analysis*[14] to determine when this condition holds. It then bypasses the unnecessary temporary Array and copy.

BLAS routines. The Basic Linear Algebra Subprograms (BLASs)[15] are the building blocks of efficient linear algebra codes. BLAS implements a variety of elementary vector-vector (level 1), matrix-vector (level 2), and matrix-matrix (level 3) operations. We have designed a Blas class as part of the Array package. It provides the functionality of the BLAS operations for the multidimensional Arrays in that package. Note that this is a 100 percent Java implementation of BLAS and not an interface to already existing native libraries. Therefore, we have a completely portable parallel implementation of BLAS that works well with the Array package. The code in the Blas class is optimized to take advantage of the internals of the Array package implementation. Application code making use of these methods will have access to tuned BLAS routines with no programming effort.

Figure 13 illustrates several features of the Array package by comparing two straightforward implementations of the basic BLAS operation dgemm. The dgemm operation computes $C = \alpha A^* \times B^* + \beta C$, where A, B, and C are matrices and α and β are scalars. A^* can be either A or A^T. The same holds for B^*. In Figure 13A the matrices are represented as doubleArray2D objects from the Array package. In Figure 13B the matrices are represented as double[ ][ ]. For simplicity, in both cases we omit the test for aliasing between C and A or B. Nevertheless, we want to emphasize that such a test is much simpler and cheaper for the Array package version.

The first difference is apparent in the interfaces of the two versions. The dgemm version for the Array package transparently handles operations on sections of a matrix. Sections are extracted by the caller and passed on to dgemm as doubleArray2D objects. Section descriptors have to be explicitly passed to the Java arrays version, using the m, n, p, i0, j0, and k0 parameters. The calling format for computing $C(0 : 9, 10 : 19) = A(0 : 9, 20 : 39) \times B(20 : 39, 10 : 19)$ using the Array package is

```
dgemm(NoTranspose,NoTranspose,1.0,
        A.section(new Range(0,9),
                  new Range(20,39)),
        B.section(new Range(20,39),
                  new Range(10,19)),0.0,
        C.section(new Range(0,9),
                  new Range(10,19)))
```

and using Java arrays is

```
dgemm(NoTranspose,NoTranspose,10,20,10,0,10,
        20,1.0,A,B,0.0,C)
```

Next, we note that the computational code in the Array package version is independent of the orien-

Figure 13 An implementation of dgemm using (A) the Array package and (B) Java arrays

```
public static void dgemm(int transa,
                         int transb,
                         double alpha,
                         doubleArray2D a,
                         doubleArray2D b,
                         double beta,
                         doubleArray2D c)
 throws NonconformingArrayException  {

 if  (transa == Transpose)
  a = a.permuteAxes(1,0);
 if (transb == Transpose)
  b = b.permuteAxes(1,0);

 int m = a.size(0);
 int n = a.size(1);
 int p = b.size(1);

 if (n != b.size(0))
  throw new NoncomformingArrayException( );
 if (p != c.size(1))
  throw new NoncomformingArrayException( );
 if (m != c.size(0))
  throw new NoncomformingArrayException( );

 for (int i=0; i<m; i++) {
   for (int j=0; j<p; j++) {
     double s = 0;
     for (int k=0; k<n; k++) {
       s += a.get(i,k)*b.get(k,j);
     }
     c.set(i,j, alpha*s+beta*c.get(i,j));
   }
 }
}
```

(A)

```
public static void dgemm(int transa,
                         int transb,
                         int m,
                         int n,
                         int p,
                         int i0, j0, k0,
                         double alpha,
                         double[] [] a,
                         double[] [] b,
                         double beta,
                         double[] [] c)  {
 if (transa != Transpose)  {
  if (transb != Transpose)  {
    for (int i=i0; i<i0+m; i++)  {
      for (int j=j0; j<j0+p; j++)  {
        double s = 0;
        for (int k=k0; k<k0+n;  k++)  {
          s += a[i][k]*b[k][j];
        }
        c[i][j] = alpha*s+beta*c[i][j];
      }
    }
  }  else  {
    for (int i=i0; i<i0+m; i++)  {
      for (int j=j0; j<j0+p; j++)  {
        double s = 0;
        for (int k=k0; k<k0+n; k++)  {
          s += a[i][k]*b[j][k];
        }
        c[i][j] = alpha*s+beta*c[i][j];
      }
    }
  }
 } else  {
       .
       .
       .
 }
}
```

(B)

tation of A or B. We just perform a (very cheap) transposition, if necessary, by creating a new descriptor for the data using the permuteAxes method. In comparison, the code in the Java arrays version has to be specialized for each combination of the orientation of A and B. (We only show the two cases in which A is not transposed.)

Finally, in the Array package version, we can easily perform some shape consistency verifications before

Figure 14 A (proposed) standard Java class for two-dimensional complex array

```
public final class ComplexArray2D  {

    private double [] data; private int n;

    public ComplexArray2D(int m, int n)  {
        data = new double[2*m*n]; this.n = n;
    }

    public Complex get(int I, int j)  {
         return new Complex(data[2*(i*n+j)],data[2*(i*n+j)+1]);
    }

    public void set(int I, int j, Complex z)  {
        data[2*(i*n+j)] = z.re;
        data[2*(i*n+j)+1] = z.im;
    }
}
```

entering the computational loop. If we pass that verification, we know we will execute the entire loop iteration space without exceptions. This verification guarantees the transactional behavior of the method. Such verifications would be more expensive for the Java arrays, because we would have to traverse each row of the array to make sure they are all of the appropriate length. Furthermore, at least the row-pointer part of each array would have to be privatized inside the method to guarantee that no other thread changes the shape of the array.

This example illustrates some of the benefits, both for the programmer and the compiler, of operating with the true multidimensional rectangular Arrays of the Array package. We summarize the benefits the Array package brings to compiler optimizations in the subsection that follows the next one.

Arrays of complex numbers. Figure 14 shows some components of class ComplexArray2D that implements two-dimensional Arrays of complex numbers. Inside the Array, values are stored in a packed form, with (*real*, *imaginary*) pairs in adjacent locations of the data array. This is similar to the FORTRAN style for representing arrays of complex numbers and only requires 16 bytes of storage per complex value. The declaration

```
ComplexArray2D a = new ComplexArray2D(m,n);
```

creates and initializes to zero an $m \times n$ Array of *complex values*, not complex objects. The equivalent structure with Java arrays would be created with

```
Complex[ ][ ] b = new Complex[m][n];
for (i=0; i<m; i++)
  for (j=0; j<n; j++)
    b[i][j] = new Complex(0, 0);
```

We note that, in the latter case, b is an array of references to Complex objects. Each entry has to be created individually and occupies a full 32 bytes.

The get operation of class ComplexArray2D returns a new Complex object with the same value as the specified Array element. The set operation assigns the value of a Complex object to the specified Array element. Semantic expansion can be used to optimize the execution of operations involving Arrays of complex numbers. In particular, the set and get operations can be recognized and translated to code that operates directly on complex values. Let us go back to the example in the subsection on the role of operator overloading that evaluates

```
b.set(i,j,a.get(i+1,j).plus(a.get(i−1,j)))
```

where a and b are objects of class ComplexArray2D. The compiler can emit code that directly retrieves the values associated with elements (i + 1, j) and (i − 1, j) of Array a, computes the sum of those values, and stores the result in element (i, j) of Array b. Not a single object creation needs to be performed.

The Array package and compiler optimizations. In this subsection we summarize the features of the Array package that play a strong role in enabling important compiler optimizations. We want to emphasize that there is a strong synergy here, since the Array package would be of little value if code using it could not be optimized to achieve high performance.

First, all classes in the Array package that implement multidimensional Arrays (e.g., intArray1D, doubleArray3D, ComplexArray2D) are final. As a result, the semantics of code using those classes are statically bound at compile time. In particular, the compiler, using semantic expansion, can recognize set and get methods and emit code that directly accesses elements of Arrays. Obviously, such code must contain the necessary checks to guarantee that the indices are in bounds. This optimization has been implemented in our research prototype compiler.[16]

Second, all Arrays in the Array package have rectangular and immutable shape. This is particularly useful for the bounds checks optimizations described in References 3 and 17. The rectangular shape of Arrays makes it trivial to identify extents along each axis. The immutability property makes it unnecessary to perform a (potentially costly) privatization to safeguard against another thread changing the shape of an Array. The rectangular shape also results in a more restrictive form of aliasing, which can be trivially disambiguated at run time. Bounds checking optimization has also been implemented in our research prototype compiler.[16]

Finally, the transactional behavior of Array operations allows them to be extensively optimized. Once the initial validation tests have been performed successfully, an Array operation always executes to the end. This implies that aggressive optimizations like loop transformations and parallelization can be applied without concern for the semantics of the operation under exceptions. The main computational part of an Array operation is totally free of exceptions.

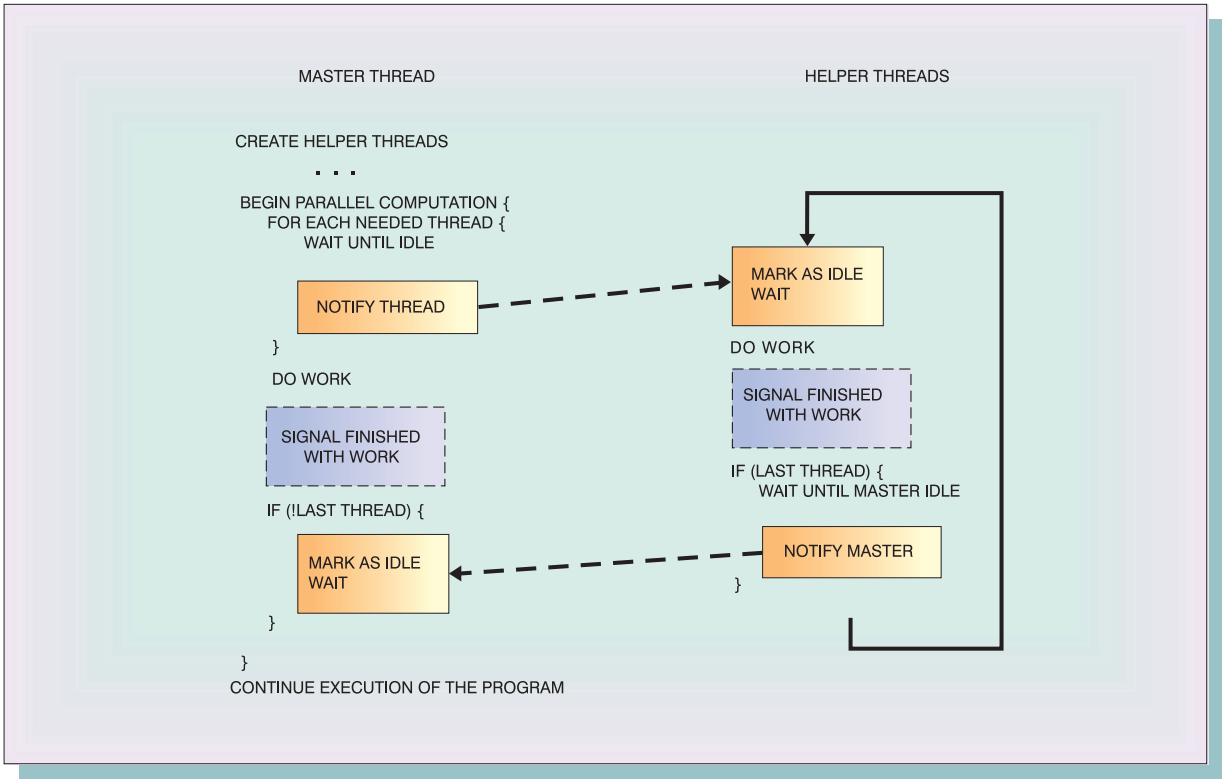
Support for implicit parallelism in the Array package. We conclude this section on the Array package by describing how the package provides support for implicit parallelism. We note that the version of the Array package in alphaWorks does not have any of the parallelism features described here. We call the version with support for parallelism the *parallel Array package*. The parallel Array package allows a user program written in a completely sequential style to obtain the performance benefits of parallelism transparently. The user program does retain control over the extent of parallelism desired by calling an initializer method of the parallel Array package that sets the number of parallel threads to be used for the application.

The parallel Array package employs a master-slave mechanism in the implicitly parallel routines and uses the multithreading facilities available in Java. Our design principles in developing this mechanism were: (1) create threads only once and reuse them in different operations; and (2) allow the master to control the assignment of work to helper threads. The first principle eliminates the cost of creating new threads for each parallel operation. The second principle supports better exploitation of data locality between operations.

Figure 15 shows the basic actions performed when an operation is executed in parallel. Solid boxes indicate mutex operations performed on per-thread data structures, and dashed boxes indicate mutex operations performed on a global shared data structure. Solid arrows indicate flow of control, and dashed arrows indicate notify events. The master thread initially creates the number of helper threads specified by an initialization call from the application program. It then begins executing the program. Each newly created helper thread marks itself as idle and waits for work on a synchronization object associated with it. This allows the Java notify method to be used to restart a specific thread.

When the master thread encounters a parallel operation, it computes T, the desired number of threads to perform the operation. It then notifies helper threads $1, \ldots, T - 1$ to start work. All of the threads, including the master, perform their part of the computation. When each thread finishes work on the parallel operation, it signals its completion by decrementing a shared counter. If the master thread is not the last thread to finish work (as can be determined by examining the shared counter to see whether it is zero), it marks itself as idle and waits

Figure 15 Overview of the thread scheduling operations



on its synchronization object. If a helper thread is the last thread to finish, it notifies the master to continue. All helper threads, when finished with the operation, mark themselves as idle and wait for the next parallel operation.

Case study: Data mining

In this section, we present a case study, using a data mining application, that illustrates some of the pitfalls and opportunities in using the Java language to develop a numerically intensive application. Data mining[18] is the process of discovering useful and previously unknown information in very large databases, with applications that span both scientific and commercial computing. Although typical data mining applications access large volumes of data from either flat files or relational databases, such applications often involve a significant amount of computation above the data access layer. High-performance data mining applications, therefore, require both fast data access and fast computation. The details of the specific data mining problem we considered are described in Appendix A.

Although Java is an attractive vehicle for developing and deploying data mining applications across different computing platforms, a major concern has been its performance. We show that this concern is well-founded but can be dealt with by using well-designed class libraries, such as the Array package described in the last section. In particular, we show that a plain Java implementation suffers from the following major performance problems, both of which are exacerbated by its lack of support for true multidimensional arrays:

- *Bounds checking and null pointer checks on array accesses*—The overhead of checking each array access for a **null** pointer or out-of-bounds access violation takes its toll on performance. To make matters worse, a single reference to a d-dimensional array in Java translates into d references to one-dimensional arrays, requiring d **null** pointer checks

and *d* out-of-bounds checks. The algorithm to optimize these checks away in a compiler by creating *safe* regions[17] is significantly simpler for a true multidimensional array because its shape is constant along all axes, and there is no need to copy arrays to the *working memory* of a thread for thread-safety of the transformation.

- *Poor data locality and instruction scheduling*—Loop transformations, such as interchange, tiling, and outer loop unrolling, typically used by optimizing compilers to improve data locality and instruction scheduling, cannot be readily applied to loops in which an exception may be thrown. This restriction is a consequence of the need to support *precise* exceptions in Java. Furthermore, different arrays constituting a multidimensional array in Java are not necessarily stored together in a single contiguous block of memory, leading to inherently poor data locality.

Using the Array package allows us to deal with these problems quite effectively. The methods in our implementation of this package perform all checks for possible exceptions before the main part of the computation. As a result, the main computation can be optimized in the same manner as equivalent FORTRAN or C++ code, while still remaining strictly Java-compliant. The main loops in the methods of the Blas class are transformed manually using well-known techniques[15] to get better uniprocessor performance through improved data locality, instruction scheduling, and register utilization. Furthermore, the Array package internally uses contiguous memory for all of the data of a multidimensional Array, leading to improved data locality and more efficient indexing of elements.

The data mining implementations. We experimented with five different implementations of the scoring algorithm described in Appendix A. The first version is a *plain* Java implementation of the scoring algorithm. That is, it does not make use of the Array package described in the previous section. Instead, it uses standard Java arrays. The second implementation is our *enhanced* Java code, which implements the scoring using classes from the Array package. The third implementation is an *implicitly* parallel version of the application that is derived from the enhanced Java code but uses the parallel Array package. The implicitly parallel Java version is identical to the enhanced Java version, except for a call at the beginning of main to an initializer method of the parallel Array package, indicating the number of threads to be used. We also derive an *explicitly* parallel version of the application, which explicitly uses the multithreading facilities in Java together with the sequential version of the Array package. Finally, we also use a FORTRAN 90 version, with calls to the Engineering and Scientific Subroutine Library (ESSL), of the scoring algorithm. The FORTRAN 90+ESSL version serves as a reference: It helps us evaluate how well Java is doing relative to a language and library known for high performance.

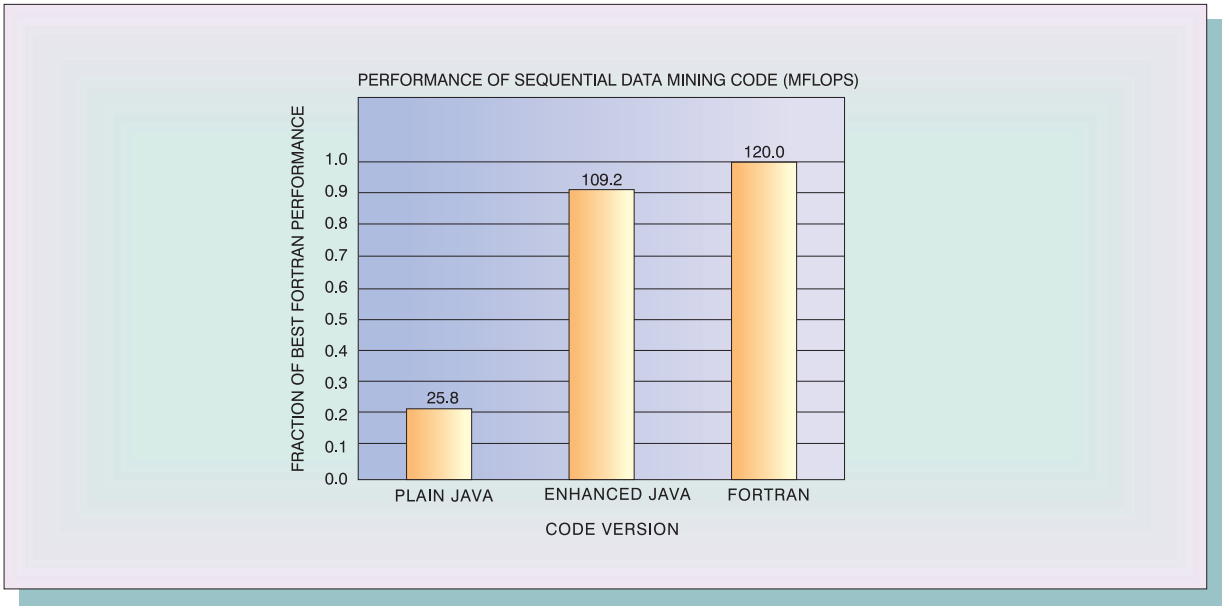
Experimental results. We now describe the performance results obtained for the different implementations of the data mining code on an IBM RS/6000* Model F50 four-way SMP (symmetric multiprocessor) using 332 MHz PowerPC 604e processors. We show the performance of the scoring algorithm, which is the bulk of the computation in the data mining code. We used the IBM XLF 6.1 compiler (with -O3 optimization level) for the FORTRAN 90 program. Results for Java code represent the best obtained using both the IBM HPCJ[2] (with -O optimization level) and IBM Java Developer Kit (DK) 1.1.6 with the IBM JIT (just-in-time) compiler. (The IBM DK with JIT compiler delivered the better performance for Java arrays, while the IBM HPCJ was better with the Array package.)

Figure 16 shows the serial performance of the Java and FORTRAN 90 codes as a fraction of the performance obtained by the FORTRAN 90 version. The numbers at the top of the bars indicate million floating-point operations per second (Mflops). The plain Java program (with Java arrays) achieves 25.8 Mflops, which is 22 percent of the FORTRAN 90 performance. The enhanced Java version (with the Array package) performs significantly better, achieving 109.2 Mflops, or 91 percent of the FORTRAN 90 performance.

Figure 17 shows the performance of the parallel codes for different numbers of threads. Again, the numbers at the top of the bars indicate Mflops. The implicitly parallel code achieves a speedup of 2.7 with four threads, reaching a performance of 292.4 Mflops. The explicitly parallel code consistently delivers better performance, achieving 343.7 Mflops on four threads, which represents a speedup of 3.1 over the enhanced Java version.

Discussion. We now present the reasons for the performance differences we have seen in the various implementations of the data mining code. We also draw some general conclusions about writing numerically intensive Java applications. Finally, we compare the

Figure 16 Performance of plain Java (Java arrays), enhanced Java (Array package), and FORTRAN 90 versions of the data mining code



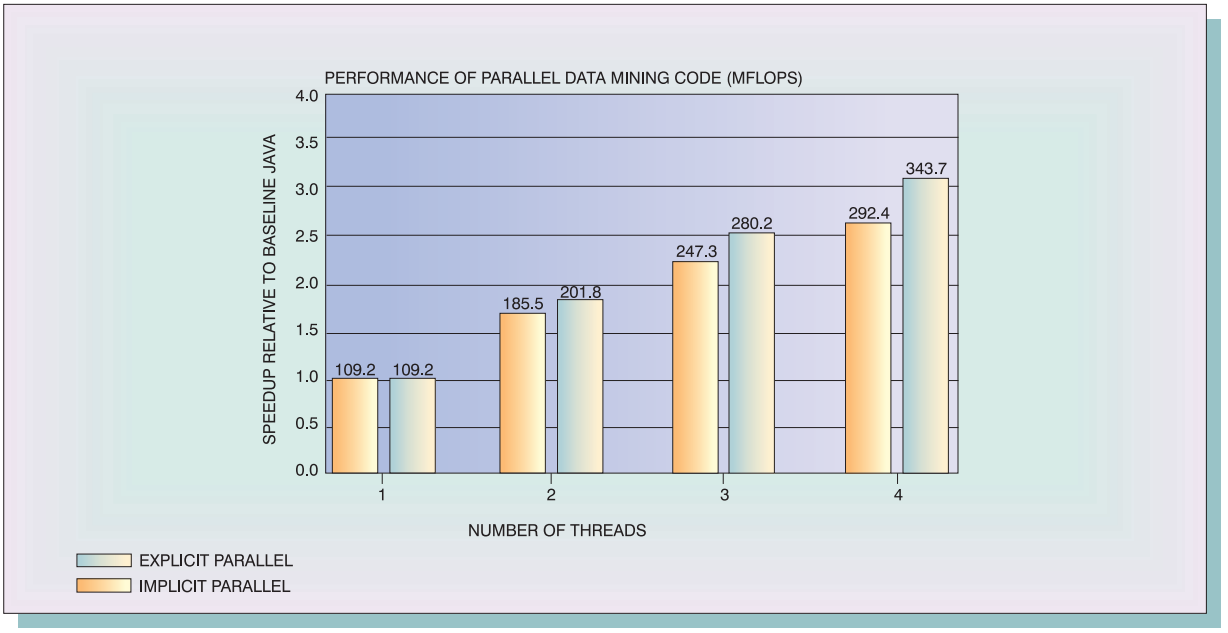
two approaches to exploiting parallelism: writing explicitly parallel code, and using a parallel subsystem to extract parallelism out of an application written in a completely sequential style.

Performance of serial versions. The Array package provides a higher level of abstraction to the programmer than the primitive operations on arrays currently defined in the Java language specification. Our experimental results demonstrate that using this package also leads to better performance. There are two main reasons for the difference in performance between the plain Java version (that uses primitive array operations) and the enhanced Java version (that uses the Array package): (1) greater negative impact of array bounds checking on the performance of the plain Java version, and (2) better data locality and instruction scheduling of the Blas class library code, used by the enhanced Java version.

In the plain Java program, bounds checking is performed for all array accesses. Since the Java language requires precise exceptions, all code-reordering transformations must be disabled in loops that have bounds checking. An additional measurement showed that the performance of this program jumps to 36.5 Mflops if all array bounds checks are optimized away. As discussed earlier, it is easier for the compiler to apply transformations[17] to deal with this problem if the program uses the Array package. In fact, for the scatter and gather operations over sparse arrays in our data mining application, static techniques, such as those discussed in Reference 17, are insufficient to optimize the bounds checks, because they cannot handle subscripted subscripts. In contrast, when using the Array package, bounds checking on an Array dimension accessed using an Index object is performed simply by comparing the minimum and maximum elements of the Index object with zero and the dimension length, respectively. The minimum and maximum elements for each Index object are computed at creation time in its constructor to enable efficient bounds checking later.

The Blas class provides the benefit of making a tuned implementation of commonly needed operations, such as matrix multiplication, available to the programmer. This is similar to the approach adopted by providers of high-performance libraries such as LAPACK[19] and ESSL.[20] As with the implementation of the rest of the Array package, all checks for conditions leading to exceptions are performed at the beginning, so that compiler optimizations can be ap-

Figure 17 Performance of explicitly parallel and implicitly parallel versions of the data mining code



plied effectively to performance-critical sections of the code.

We observe that by using the Array package, which does not use any native libraries, the Java version of the data mining code achieves a level of performance close to that delivered by the FORTRAN 90+ESSL version. Thus, we show that it is possible to obtain competitive performance, even on a numerically intensive production quality code, with pure Java.

Performance of parallel versions. Our experiments with explicitly parallel and implicitly parallel implementations of the data mining code show that it is possible to get the benefits of parallelism by simply using the parallel version of the Array package, and that manual parallelization of an application can typically achieve higher performance than a purely library-based approach. Manual parallelization is more amenable to global decisions that increase opportunities for exploiting parallelism and reduce the overhead of parallelization.

The support for implicit parallelism in our implementation of the Array package entirely hides the complexity of parallelization from the end user. The user merely has to specify the degree of parallelism desired. In contrast, the implicitly parallel code suffers from four main sources of performance degradation relative to the explicitly parallel code: (1) higher overhead of threading operations, (2) greater load imbalance, (3) more serial components, and (4) poorer cache utilization and a greater amount of cache traffic from interference in shared data. These factors are largely a consequence of the fact that the implicitly parallel code exploits parallelism at a finer granularity than the explicitly parallel code. The explicitly parallel version has a single dominant parallel outer loop. The overhead of waking up helper threads and waiting for them to finish is incurred only once, and a bigger section of the code is parallelized. Additionally, most of the temporary Arrays used in the explicitly parallel code are read and written by a single thread, so that this version attains very good cache utilization and avoids the problems of cache line invalidations resulting from false sharing. The implicitly parallel code, by its very nature, relies on library calls over shared data.

We observe that even though the implicitly parallel approach does not lead to the best possible performance, it consistently delivers good performance as the number of threads is increased. On four proces-

sors, it leads to a respectable speedup of 2.7 over the sequential code, as compared with a speedup of 3.1 obtained using the explicitly parallel approach. For many users, this performance level would be acceptable, given the ease with which it is obtained.

Case study: MICROSTRIP

Our second case study comes from the (much simplified) electromagnetics application MICROSTRIP.[21] This example is representative of many applications that deal with physical phenomena. It implements a numerical iterative solver for the partial differential equation that describes the behavior of a physical system. MICROSTRIP makes heavy use of complex arithmetic. We use it to illustrate some additional Java performance issues, not discussed in the data mining case study:

- *Complex numbers*—Java does not support complex numbers as primitive types. The typical approach is to define a Complex class and then use Complex objects to implement complex numbers. We will see that this approach leads to enormous object creation and destruction overhead.
- *Storage efficiency*—This issue is related to implementing complex numbers as Complex objects. Each Complex object includes, in addition to the double fields for the real and imaginary parts, data that describe the object. It results in a 100 percent storage overhead. Also, Java arrays of Complex (e.g., Complex[ ],Complex[ ][ ]) are actually arrays of *references* to Complex objects. This leads to poor memory locality and poor memory system performance.

In the case of MICROSTRIP, we achieve high performance through a combination of semantic expansion (discussed earlier) and features of the Array package. Semantic expansion is a compilation technique that replaces method calls by code that directly implements the semantics of those methods. This technique allows us to support complex numbers in Java as efficiently as in FORTRAN. The Array package has a strong synergy with semantic expansion. Multidimensional Arrays of complex numbers (e.g., ComplexArray1D and ComplexArray2D) deliver better locality than Java arrays of Complex objects. However, semantic expansion is absolutely necessary to allow efficient access to elements of these arrays.

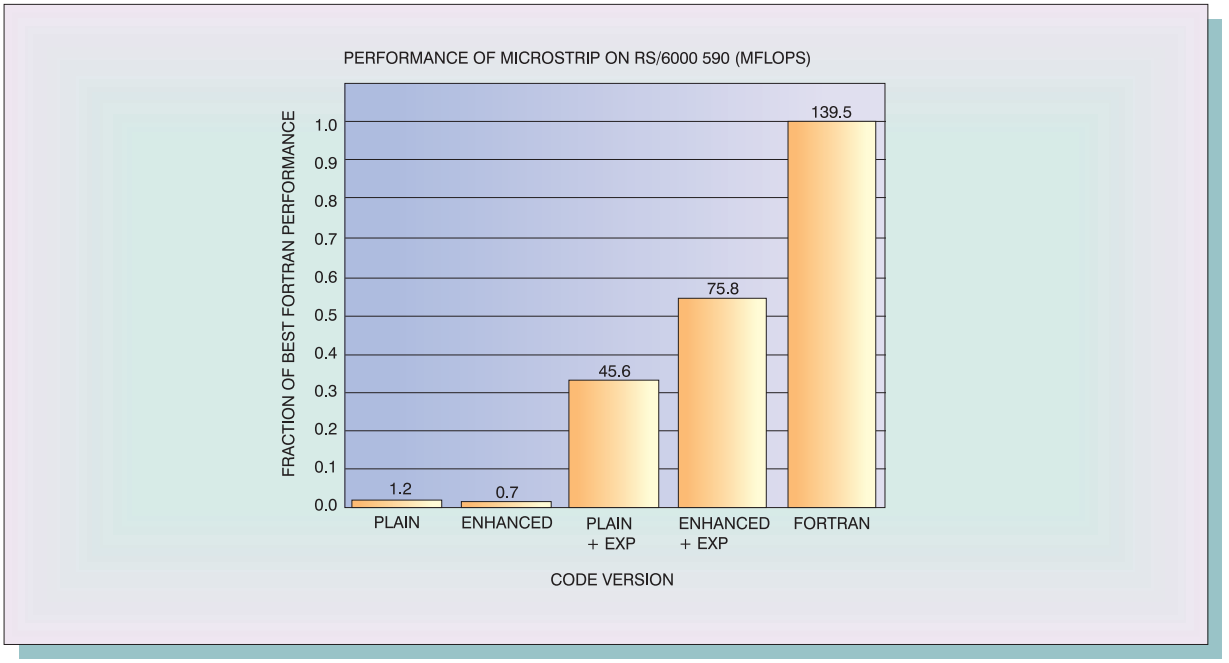
The MICROSTRIP implementations. We experimented with three different implementations of the iterative solver for MICROSTRIP. The first version is a *plain* Java implementation that uses Java arrays of Complex objects. The second implementation is our *enhanced* Java code that uses classes from the Array package. Each of the two Java versions can be compiled with or without the semantic expansion technique. As we shall see in the following subsection, semantic expansion has a significant impact on performance. Finally, we use a FORTRAN 90 version of the solver, which serves as a yardstick for evaluating the performance of Java. This FORTRAN version achieves approximately 50 percent of the peak performance of our benchmark machine. (It achieves 140 out of a 266 peak Mflops.) Therefore, it constitutes a good reference point against which we compare our Java performance.

Experimental results. We now discuss the performance results obtained for the different implementations of the MICROSTRIP code on an IBM RS/6000 Model 590 workstation. This machine has a 67-MHz POWER2* processor with a 256-KB single-level data cache and 512 MB of main memory. The peak computational speed is 266 Mflops. To execute the Java versions, we used both the IBM HPCJ (with -O optimization level) and IBM DK 1.1.8 with the IBM JIT compiler. (We report the best result achieved in each case.) We used the IBM XLF 6.1 compiler (with -O3 optimization level) for the FORTRAN version.

Figure 18 shows five different results for the MICROSTRIP benchmark. The problem parameters are those described in Reference 21 and Appendix B. The numbers at the top of the bars indicate Mflops. The bars labeled "plain" and "enhanced" show the performance for the plain (Java arrays) and enhanced (Array package) Java implementations, respectively, *without* semantic expansion. (The best results for these cases were achieved with IBM DK 1.1.8.) Both versions achieve approximately 1 Mflop. This performance would typically be delivered by current Java environments. The bars "plain + exp" and "enhanced + exp" show the performance for the plain and enhanced Java implementations, respectively, *with* semantic expansion (using our research prototype compiler). The plain Java version achieves 45.6 Mflops with semantic expansion, whereas the enhanced Java version achieves 75.8 Mflops. Finally, the bar labeled "FORTRAN" shows the performance of the FORTRAN implementation. The FORTRAN version achieves 139.5 Mflops, or 52 percent of the peak computational speed of the machine.

Discussion. We now discuss why the performance of the Java versions without semantic expansion is so poor. We also discuss why, with semantic expan-

Figure 18 Summary of results for MICROSTRIP; the "+ exp" notation indicates use of semantic expansion



sion, the performance of the enhanced Java version is better than the plain version. We note that the synergy between the Array package and semantic expansion leads to pure Java performance that is a respectable 55 percent of the best FORTRAN performance we can achieve.

Java without semantic expansion. Coding the iterative solver using Java arrays leads to very poor performance in current implementations of Java. The reason is that each arithmetic operation (e.g., methods plus and times) creates a new Complex object to represent the results. (See Figure 3.) Object creation is a very expensive operation and causes the plain Java version of MICROSTRIP to be approximately 100 times slower than the reference FORTRAN version.

The ComplexArray2D class offers a significant storage benefit compared to Complex[ ][ ], since it only stores complex values and not Complex objects (a 50 percent reduction in storage and associated improvements in memory bandwidth and cache behavior). The performance of numerical codes that use ComplexArray2D, however, is just as bad as codes that use Java arrays of Complex objects. Execution continues to be dominated by object creation and destruction. In fact, every get operation on a ComplexArray2D results in a new temporary object. The performance of this enhanced version on current Java environments is approximately 200 times slower than the reference FORTRAN.

Java with semantic expansion. The benefits of treating complex numbers as values rather than objects are enormous. We were able to increase the performance 40- and 100-fold for the plain and enhanced versions, respectively. Of particular importance is the synergy between the Array package and semantic expansion. By eliminating the cost of creating temporary objects, semantic expansion makes the use of ComplexArray2D objects viable from a performance perspective. ComplexArray2D, in turn, delivers better memory behavior than Java arrays of Complex objects. The combination of the two approaches delivers a Java performance on a complex arithmetic application that is 55 percent of the best FORTRAN performance.

Additional experiments

We performed additional experiments to further illustrate the performance impact of our techniques

for optimizing Java numerical codes. In this section we present a summary of results from eight benchmarks. Four of these benchmarks perform real arithmetic, and the other four complex arithmetic. We compare the performance of Java and FORTRAN versions of the benchmarks. We perform all our experiments on an IBM RS/6000 Model 590 workstation. This machine has a 67-MHz POWER2 processor with a 256-KB single-level data cache and 512 MB of main memory. The peak computational speed is 266 Mflops.

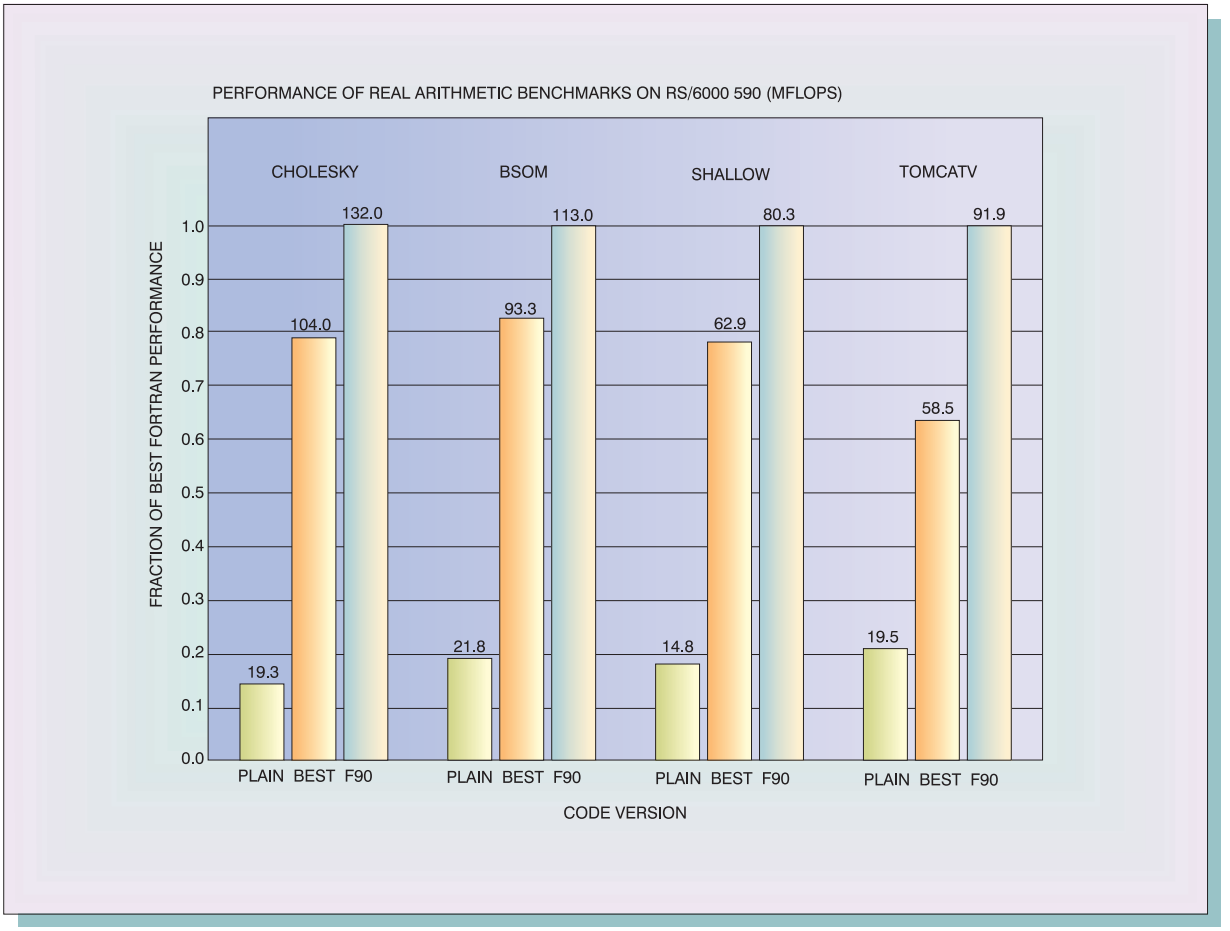
FORTRAN programs are compiled using version 6.1 of the IBM XLF compiler with the highest level of optimization (-O3 -qhot, which performs high-order loop transformations[4]). Results for two different Java versions of each benchmark are reported. One version, which we call *plain*, is an implementation of the benchmark using Java arrays. The numbers reported for this version correspond to the best obtained using IBM DK 1.1.8 with the IBM JIT compiler. (The JIT compiler, which incorporates many advanced optimizations such as bounds checking and **null** pointer checking elimination, performs better than HPCJ when Java arrays are used.) The other Java version, which we call *best*, represents the best result we achieved from a pure Java implementation of the benchmark. It uses multidimensional Arrays from the Array package and aggressive compiler optimizations in our research prototype version of IBM HPCJ to generate safe regions of code (i.e., regions without potential exceptions) and perform semantic expansion. For the real arithmetic benchmarks, we also enabled the use of the fused-multiply add (fma) instruction of the POWER2 hardware for both the Java and FORTRAN versions of the benchmark (the default for FORTRAN is to use the fma). This represents the performance that can be achieved with Java if the current proposals for relaxed floating-point arithmetic are approved.[1] Because of some technical difficulties, we could not enable the use of the fma in Java for the complex arithmetic benchmarks. In that case, we chose to also disable the use of fma in FORTRAN.

To guarantee a fair comparison, all three versions of each benchmark (FORTRAN, Java arrays, and Array package) were automatically generated from a common representation. We use an internally developed language, *z*-code—a very simplified FORTRAN-like language, to code each of the benchmarks. From the representation in *z*-code, an automatic translator generates all three versions of a benchmark. The translator takes care of adjusting array indexing to guarantee that arrays are accessed in their preferred mode (column-major for FORTRAN and row-major for Java).

Real arithmetic benchmarks. The real arithmetic benchmarks are: CHOLESKY, BSOM, SHALLOW, and TOMCATV. CHOLESKY is a straightforward implementation of the Cholesky decomposition algorithm, as described, for example, in References 22 and 23. It computes the upper triangular factor U of a symmetric positive definite matrix A such that $A = U^T U$. We implemented our code so that the factorization is performed in place, with the upper half of matrix A being replaced by the factor U. For our experiments, we factor a matrix of size 1000×1000. The BSOM (batch self-organizing map) benchmark is a data-mining kernel representative of technologies incorporated into Version 2 of the IBM Intelligent Miner*. (It was not used in the data mining application described earlier.) It implements a neural-network-based algorithm to determine clusters of input records that exhibit similar attributes of behavior. We time the execution of the *training* phase of this algorithm, which actually builds the neural network. This phase consists of 25 *epochs*. Each epoch updates a neural network with 16 nodes using 256 records of 256 fields each. SHALLOW is a computational kernel from a shallow water simulation code from the National Center for Atmospheric Research. The data structures in SHALLOW consist of 14 matrices (two-dimensional arrays) of size $n \times m$ each. The computational part of the code is organized as a time-step loop, with several array operations executed in each time step. For our measurements, we fix the number of time steps $T = 20$ and use $n = m = 256$. TOMCATV is part of the SPECfp95 suite (available at http://www.spec.org). It is a vectorized mesh generation with Thompson solver code. The benchmark consists of a main loop that iterates until convergence or until a maximum number of iterations is executed. At each iteration of the main loop, the major computation consists of a series of stencil operations on two (coupled) grids, X and Y, of size $n \times n$. In addition, a set of tridiagonal systems is solved through LU decomposition. For our experiments, we use a problem size of $n = 513$.

Results for these four benchmarks are summarized in Figure 19. The height of each bar is proportional to the best FORTRAN performance achieved in the corresponding benchmark. The numbers at the top of the bars indicate actual Mflops. For the "plain" Java version, two-dimensional arrays of doubles were represented using a Java double[ ][ ] array. The "best" Java version uses doubleArray2D Arrays from the Array

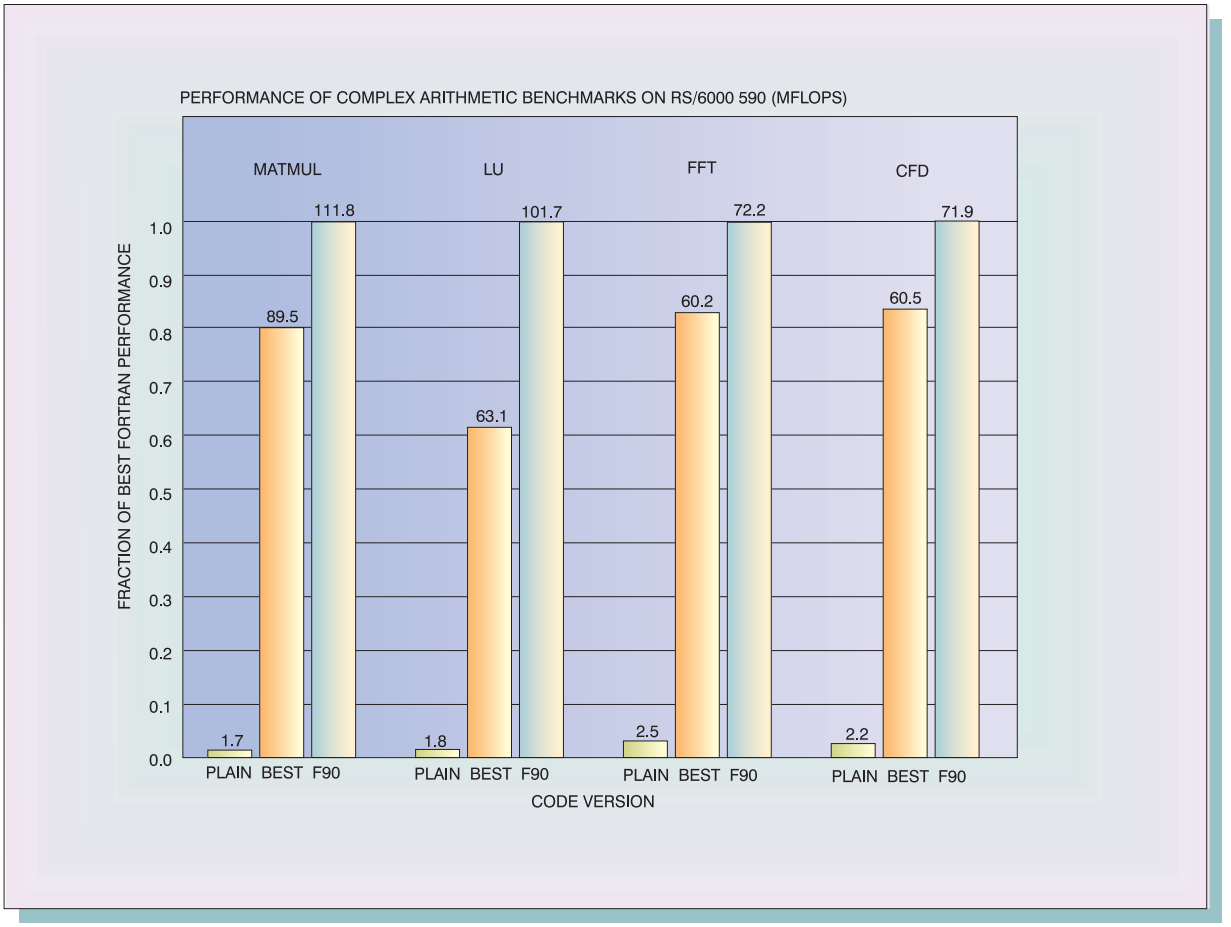
Figure 19 Summary of experimental results for real arithmetic benchmarks CHOLESKY, BSOM, SHALLOW, and TOMCATV



package. The use of multidimensional Arrays from the Array package in turn enables bounds checking and other optimizations. In all cases we observe significant performance improvements between the "plain" and "best" Java versions. Improvements range from a factor of 2.5 (19.5 to 58.5 Mflops for TOMCATV) to a factor of 5 (19.3 to 104 Mflops for CHOLESKY). We achieve Java performance that ranges from 65 percent (TOMCATV) to 80 percent (CHOLESKY, BSOM, and SHALLOW) of fully optimized FORTRAN code.

Complex arithmetic benchmarks. The complex arithmetic benchmarks are: MATMUL, LU, FFT, and CFD. MATMUL computes $C = C + A \times B$, where C, A, and B are complex matrices of size 500×500. We use a dot-product version of matrix multiplication, with an i-, j-, k-loop nest. The i, j, and k loops are blocked and the i and j loops are unrolled, in all versions, to improve performance.[4] LU is a straightforward implementation of Crout's algorithm[22,23] for performing the LU decomposition of a square matrix A, with partial pivoting. The factorization is performed in place and, in the benchmark, A is of size 500×500. FFT computes the discrete Fourier transform of a two-dimensional complex function, represented by an $n \times m$ complex array. We use the Daniel-Lanczos method described in Reference 23 to compute the one-dimensional FFTs in the two-dimensional FFT. For our experiments we use $n = m = 256$. CFD is a kernel from a computational fluid dynamics application. It performs three convolutions

Figure 20 Summary of experimental results for complex arithmetic benchmarks MATMUL, LU, FFT, and CFD



between pairs of two-dimensional complex functions. Each function is represented by an $n \times m$ complex array. The computation performed in this benchmark is similar to a two-dimensional version of the NAS Parallel Benchmark FT. Again, for our experiments we use $n = m = 256$.

Results for these four benchmarks are summarized in Figure 20. Again, the height of each bar is proportional to the best FORTRAN performance achieved in the corresponding benchmark, and the numbers at the top of the bars indicate actual Mflops. For the "plain" Java version, complex arrays were represented using a Complex[ ][ ] array of Complex objects. No semantic expansion was applied. The "best" Java version uses ComplexArray2D Arrays from the Array package and semantic expansion. In all cases we observe significant performance improvements between the "plain" and "best" Java versions. Improvements range from a factor of 24 (2.5 to 60.2 Mflops for FFT) to a factor of 53 (1.7 to 89.5 Mflops for MATMUL). We achieve Java performance that ranges from 60 percent (LU) to 85 percent (FFT and CFD) of fully optimized FORTRAN code.

Related work

The importance of having high-performance libraries for numerical computing in the Java language has been recognized by many authors. In particular, References 24–26 describe projects to develop such libraries entirely in Java. In addition, there are approaches in which access to existing numerical libraries (typically coded in C and FORTRAN) is pro-

vided to Java applications.[27–29] The Array package includes a Blas class, so that efficient linear algebra libraries can be developed for it.

It is well known that programming with libraries has its limitations. Certain classes of applications can be effectively expressed in terms of linear algebra operations. These applications can be efficiently implemented on top of (very successful) linear algebra libraries such as LAPACK and ESSL. Other classes of applications are not so well-structured. In those cases, the programmer has to develop the application from scratch, counting on minimal library support. For this reason, the Array package is more than just a library: It is a mechanism to represent array operations in a manner that can be highly optimized by compilers. Linear algebra code can be developed with the Array package using the BLAS primitives. Less-structured code can use the Array operations directly. With the appropriate compiler support, Java code built on top of the most basic set and get operations of the Array package can achieve FORTRAN-like performance.

Cierniak and Li[30] describe a global analysis technique for determining that the shape of a Java array of arrays (e.g., double[ ][ ]) is indeed rectangular and not modified. The array representation is then transformed to a dense storage, and element access is performed through index arithmetic. This approach can lead to results that are as good as those obtained from using multidimensional Arrays in the Array package. We differ in that we do not need global analysis: Arrays from the Array package are intrinsically rectangular and can always be stored in a dense form. We have also integrated support for complex numbers in our true multidimensional Arrays.

The technique of semantic expansion we use is similar to the approach taken by FORTRAN compilers in implementing some *intrinsic* procedures.[11] Intrinsic procedures can be treated by the FORTRAN compiler as language primitives, just as we treated the Complex class in Java. Semantic expansion differs from the handling of intrinsics in FORTRAN in that both new data types and operations on the new data types are treated as language primitives. Still regarding semantic expansion, the work by Wu and Padua[31] targets standard container classes for semantic expansion. In their paper, the container semantics are not used for local optimizations or transformations inside the container. Instead, the semantics are used to help data flow analysis and detect parallelizable loops. Their work illustrates how semantic information about standard classes exposes new optimization and parallelization opportunities.

Array operations are natural candidates for the exploitation of parallelism. Exploiting parallelism has been done extensively before both at the language[32–34] and subsystem[12,35,36] levels, with different degrees of transparency to the application programmer. So far, we have successfully exploited parallelism inside the Array package operations while achieving total transparency to the programmer. A combination of the Array package with semantic expansion can lead to programs that are amenable to automatic parallelization using techniques developed, for example, for FORTRAN. This will result in transparent parallelization of the user code itself.

The efficacy of the Array package in supporting applications of a varied nature is demonstrated by the results described in the sections containing the two case studies and the additional experiments. The strong synergy between the Java Array package for multidimensional Arrays and the aggressive compiler optimizations is the main differentiator in our work.

Conclusion

We have demonstrated that high-performance numerical codes can be developed in the Java language. The benefits of using Java from a productivity and demographics point of view have been known for a while. Many people have advocated the development of large, computationally intensive Java applications based on those benefits. However, Java performance has consistently been considered an impediment to its applicability to numerical codes. This paper has presented a set of techniques that lead to Java performance that is competitive with the best FORTRAN implementations available today.

We have used a class library approach to introduce in Java features of FORTRAN 90 that are of great importance to numerical computing. These features include complex numbers, multidimensional arrays, and libraries for linear algebra. These features have a strong synergy with the compiler optimizations that we have developed, particularly bounds checking optimization and semantic expansion. We have demonstrated this synergy, and the resulting performance impact, through two detailed case studies. We have also conducted a broader performance evaluation using eight other numerical benchmarks.

We demonstrated that we can deliver Java performance in the range of 55–90 percent of the best

FORTRAN performance for a variety of benchmarks. This step is very important in making Java the preferred environment for developing large-scale numerically intensive applications. However, there is more than just performance to our approach. The Array package and associated libraries create a Java environment with many of the features that experienced FORTRAN programmers have grown accustomed to. This combination of delivering features *and* performance for numerical computing in the context of the Java language is the core of our approach to making Java the environment of choice for new numerical computing.

Regarding future work, we want to exploit more of the benefits generated by the Array package. One of our goals is automatic parallelization of user code developed with the Array package. We can leverage many techniques developed for parallelizing FORTRAN and C, but good alias disambiguation is essential. We are currently implementing alias disambiguation techniques in our compiler, taking advantage of the semantics of the Array package. Another area we are exploiting is data layout optimization. By hiding the actual layout of data from the user (elements can only be accessed through get and set accessor methods), the Array package facilitates optimizations of this layout. In particular, we are pursuing the use of recursive block formats,[6] which can be very beneficial in systems with deep memory hierarchies. By taking advantage of these and other optimizations, we can envision a future not too distant in which Java numerical codes will actually outperform their FORTRAN counterparts.

Acknowledgments

The authors wish to thank Ven Seshadri of IBM Canada for helping and supporting our experiments with HPCJ.

Appendix A: The data mining computation

The specific data mining problem considered here involves recommending new products to customers based on previous spending behavior. As input, we have available both detailed purchase data for the customer set, as well as a product taxonomy that generates assignments of each product to spending categories. In the specific application discussed here, we utilize approximately two thousand such categories. Recommendations are drawn from a subset of eligible products. For each customer, a personalized recommendation list is generated by sorting this list of eligible products according to a customer-specific score computed for each product. In some commercial situations, there may be an incentive to preferentially recommend some products over others because of overstocks, supplier incentives, or increased profit margins. This information can be introduced into the recommendation strategy via product-dependent scaling factors, with magnitudes reflecting the relative priority of recommendation. We now give a more precise description of the scoring algorithm.

Let there be m products eligible for recommendation, p customers, and n spending categories. Each product i has associated with it an *affinity vector* A_i, where A_{ik} is the affinity of product i with spending category k. These affinities can be interpreted as the perceived appeal of this product to customers with participation in this spending category. They are determined by precomputing associations[37] at the level of spending categories. The collection of affinity vectors from all products forms the $m \times n$ affinity matrix A. This matrix is sparse and organized so that products with the same nonzero patterns in their affinity vectors are adjacent. The matrix is shown in Figure 21. Because of this organization, matrix A can be represented by a set of γ groups of products. Each group i is defined by f_i and l_i, the indices of the first and last products in the group, respectively. All products with the same nonzero pattern belong to the same group. This nonzero pattern for the products in group i is represented by an index vector I_i, where I_{ik} is the position of the kth nonzero entry for that group. Let $\text{len}(I_i)$ be the length of index vector I_i. Also, let $g_i = l_i - f_i + 1$ be the number of products in group i. Then the affinity matrix G_i for group i is the $g_i \times \text{len}(I_i)$ dense matrix with only the nonzero entries of rows f_i to l_i of A. This representation of A is shown in Figure 21.

Each customer j has an associated *spending vector* S_j, where S_{jk} is the normalized spending of customer j in category k. The collection of spending vectors of all customers forms the $p \times n$ spending matrix S. This matrix is also sparse, but customers are not organized in any particular order. (The affinity matrix is relatively static and can be built once, whereas the spending matrix may change between two executions of the scoring algorithm.) We also define a $p \times n$ normalizing matrix N, which has the same nonzero pattern as S, but with a one wherever S has a nonzero:

Figure 21 Structure and representation of the affinity matrix *A*

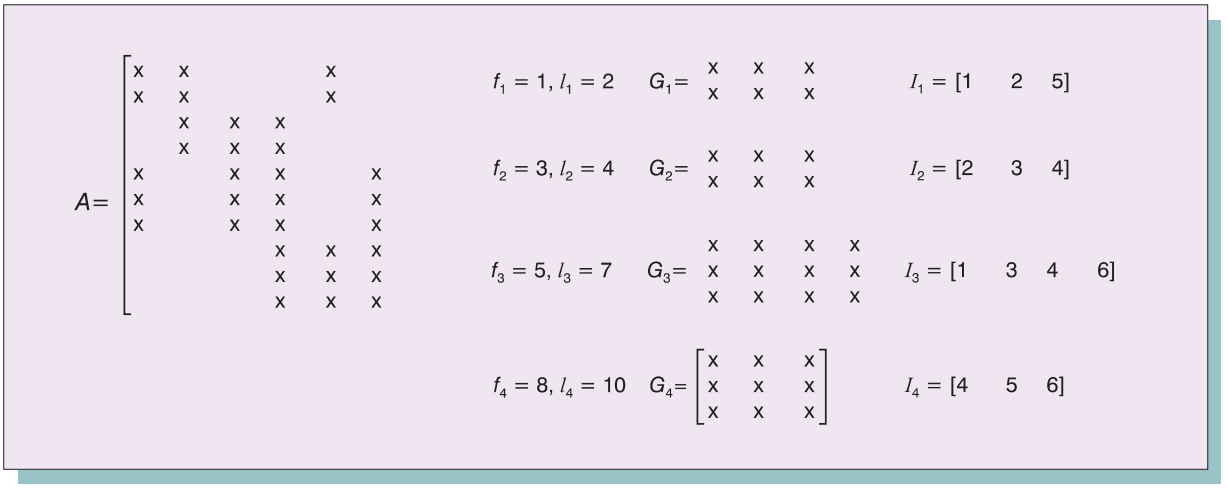
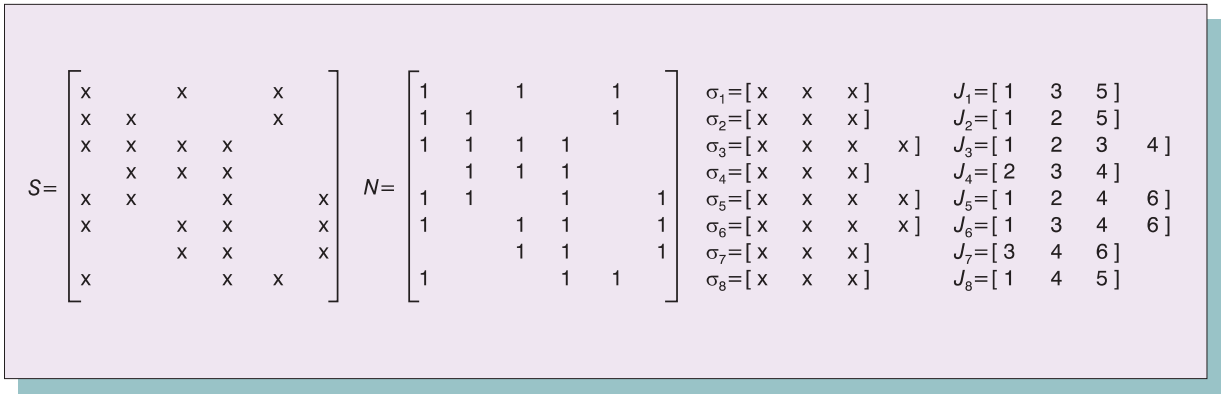


Figure 22 Structures of the spending matrix *S* and normalizing matrix *N*, and representation of matrix *S*



$$N_{jk} = \begin{cases} 1 & \text{if } S_{jk} \neq 0 \\ 0 & \text{if } S_{jk} = 0 \end{cases} \tag{3}$$

The structure of matrices S and N are shown in Figure 22. The nonzero pattern of row j of matrix S is represented by an index vector J_j, where J_{jk} is the position of the kth nonzero entry for that row (customer). The actual spending values are represented by a dense vector σ_j, of the same length as J_j, which has only the nonzero entries for row j of S. This representation of S is shown in Figure 22. Matrix N does not have to be represented explicitly.

Let ρ_i be the priority scaling factor for product i as discussed earlier in this appendix. The *score* Φ_{ij} of customer j against product i is computed as:

$$\Phi_{ij} = \rho_i \frac{\sum_{k=1}^{n} A_{ik} S_{jk}}{\sum_{k=1}^{n} A_{ik} N_{jk}} \tag{4}$$

Note that $\Sigma_{k=1}^{n} A_{ik} S_{jk}$ is the dot-product of row i of A by column j of S^T. Similarly, $\Sigma_{k=1}^{n} A_{ik} N_{jk}$ is the dot-product of row i of A by column j of N^T. Let $\Lambda_p(\rho_1, \rho_2, \ldots, \rho_m)$ denote an $m \times p$ matrix Λ with

Table 1 Problem parameters for our data mining application

Matrix	Size (Rows × Columns)	Number of Nonzeros	Fraction of Nonzeros
A	10 350 × 2103	397 559	1.83%
S	4 800 × 2103	231 194	2.29%
Φ	10 350 × 4800	20 759 569	41.79%

$\Lambda_{ij} = \rho_i$, $1 \le i \le m$, $1 \le j \le p$. Then, Equation 4 can be rewritten as a matrix operation:

$$\Phi = \Lambda_p(\rho_1, \rho_2, \ldots, \rho_m) * (A \times S^T) \div (A \times N^T) \quad (5)$$

where $\times$ denotes matrix multiplication, $\div$ denotes two-dimensional array (or element-by-element) division, and $*$ denotes two-dimensional array (element-by-element) multiplication.

Using the representations of A and S discussed previously, the scores for a customer j against all products in a product group i can be computed in the following way. First, two vectors ε and η of size n are initialized to zero:

$$\varepsilon[1 : n] = 0$$
$$\eta[1 : n] = 0 \quad (6)$$

Then, the compressed vector σ_j is expanded by assigning its values to the elements of ε indexed by J_j. (This is a scatter operation.) Similarly, an expanded representation of the jth row of N is stored into η:

$$\varepsilon[J_j] = \sigma_j$$
$$\eta[J_j] = 1 \quad (7)$$

Now, the scores of customer j against products f_i to l_i can be computed by:

$$\Phi[f_i : l_i, j] = \Lambda_1(\rho_{f_i}, \rho_{f_i+1}, \ldots, \rho_{l_i}) * (G_i \times \varepsilon[I_i]) \div (G_i \times \eta[I_i]) \quad (8)$$

where $\times$ now denotes matrix-vector multiplication, and $\div$ and $*$ denote one-dimensional array (element-by-element) division and multiplication, respectively. Note that we have two gather operations, in $\varepsilon[I_i]$ and $\eta[I_i]$. If we group several customers together, forming a block from customer j_1 to customer j_2, the operations in Equation 8 become dense matrix multiplications, array division, and array multiplication:

$$\Phi[f_i : l_i, j_1 : j_2] = \Lambda_{j_2-j_1+1}(\rho_{f_i}, \rho_{f_i+1}, \ldots, \rho_{l_i}) * (G_i \times \varepsilon[I_i, j_1 : j_2]) \div (G_i \times \eta[I_i, j_1 : j_2]) \quad (9)$$

Matrix multiplication can be implemented more efficiently than matrix-vector multiplication. This is particularly true on cache-based RISC (reduced instruction set computing) microprocessors, since matrix multiplication can be organized through blocking to better exploit the memory hierarchy.

In our experiments, the affinity matrix A is stored as a set of 93 dense blocks, each block representing a distinct group. The S matrix is stored in compressed rows. Finally, the Φ matrix, because of its relatively large number of nonzeros, is stored in expanded form. We used the problem parameters shown in Table 1.

Appendix B: The MICROSTRIP computation

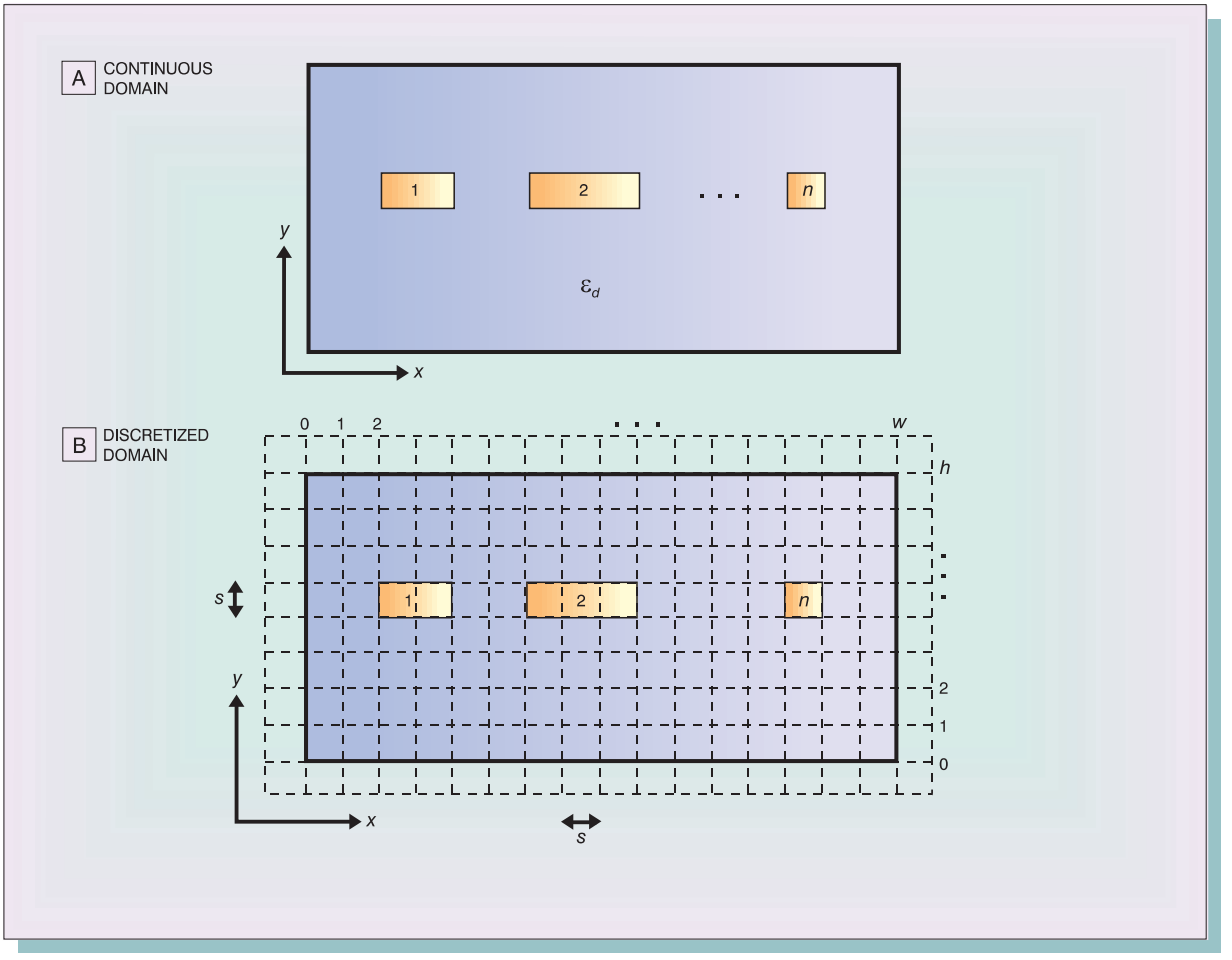
In a shielded microstrip structure (see Figure 23A), n parallel microstrips run inside a homogeneous insulator. A conducting shield, at a reference potential $V_{\text{shield}} = 0$, completely encloses the structure. Each microstrip k is at a voltage V_k with respect to the shield. We want to compute the value of the potential field $\Phi(x, y)$ in each point of the structure. The potential field $\Phi(x, y)$ is described by a partial differential equation.

The first step in computing a numerical solution for the field $\Phi(x, y)$ is to discretize the problem domain through a rectangular *grid* of evenly spaced points. Figure 23B illustrates this discretization. The grid has shape $(w + 1) \times (h + 1)$, and s is the *grid step*, or space between consecutive grid points. Points in the structure can be identified by their coordinates in the grid. We use the notation $\Phi_{i,j}$ to denote the value of the potential field in point (i, j) of the grid. Using the discretization, and applying several simplifications to the physics of the problem, we arrive at the following equation for the potential field:

$$\Phi_{i+1,j} + \Phi_{i-1,j} + \Phi_{i,j+1} + \Phi_{i,j-1} - 4\Phi_{i,j} = 0 \quad (10)$$

for all points (i, j) of the insulator. This, in fact, corresponds to a system of equations in the unknown $\Phi_{i,j}$ for all i and j. One approach to solving such a

Figure 23 A shielded MICROSTRIP structure



system is through an iterative method called *Jacobi relaxation*. We start with some arbitrary initial approximation of the potential field, $\Phi^0_{i,j}$, for all points (i, j). (The values on the microstrips and the shield are fixed by the problem boundary conditions.) Then, for each point (i, j), we compute a better approximation of the solution through the expression

$$\Phi^1_{i,j} = \frac{1}{4}\left(\Phi^0_{i+1,j} + \Phi^0_{i-1,j} + \Phi^0_{i,j+1} + \Phi^0_{i,j-1}\right) \qquad (11)$$

In the next iteration of the method we compute an even better approximation:

$$\Phi^2_{i,j} = \frac{1}{4}\left(\Phi^1_{i+1,j} + \Phi^1_{i-1,j} + \Phi^1_{i,j+1} + \Phi^1_{i,j-1}\right) \qquad (12)$$

We continue this process until we converge to some satisfactory solution. (A typical condition is that we want the difference between Φ^k and Φ^{k+1} to be very small.) From a programming point of view, we represent the field by two arrays, a and b, of size $(w + 1) \times (h + 1)$. We can then write the relaxation step as

for $i = 1, 2, \ldots, w - 1$
  for $j = 1, 2, \ldots, h - 1$
    $b(i, j) = \frac{1}{4}(a(i + 1, j) + a(i - 1, j)$
      $+ a(i, j + 1) + a(i, j - 1))$ (13)
  end
end

where a is used to represent the current value of the potential field Φ and b its next value. We are interested in the case where Φ is a complex-valued func-

Figure 24 Iterative solver for MICROSTRIP

```
while (error>e)

 (*relaxation step*)
 for i = 1,2,...,w–1
    for j = 1,2,...,h–1
       b(i,j) = ¼(a(i+1,j)+a(i–1,j)+a(i,j+1) + a(i,j–1))
    end
 end

 (*another relaxation step, to put things back into a*)
 for i = 1,2,...,w–1
    for j = 1,2,...,h–1
       a(i,j) = ¼(b(i+1,j)+b(i–1,j)+b(i,j+1)+b(i,j–1))
    end
 end

 (*error computation*)
 error = 0
 for i = 0,1,...,w
    for j = 0,1,...,h
       error = error+abs(b(i,j)–a(i,j))
    end
 end
 error = error/((w+1) x (h+1))
end
```

tion. We can measure progress in our iterative solver by computing the error between the previous and current approximation for Φ as follows:

$$
\begin{aligned}
&\text{error} = 0\\
&\textbf{for } i = 0, 1, \ldots, w\\
&\quad \textbf{for } j = 0, 1, \ldots, h\\
&\qquad \text{error} = \text{error} + \textbf{abs}(b(i, j) - a(i, j)) \qquad (14)\\
&\quad \textbf{end}\\
&\textbf{end}\\
&\text{error} = \text{error}/((w + 1) \times (h + 1))
\end{aligned}
$$

The entire iterative solver is a combination of relaxation steps and error computation, as shown in Figure 24. For clarity, we omit the code that handles the boundary conditions at the microstrips. Although important, that code represents only a small fraction of the computation. The interested reader can obtain more detailed information from Reference 21. For the particular problem computed in the MICROSTRIP benchmark, the grid size is 1000×1000 and there are four microstrips, each of cross section 100×10 grid steps, running through the insulator.

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